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#### THEORETICAL ANALYSIS OF A MODEL FOR A FIELD DISPLACEMENT ISOLATOR

Ram Sharon

# NAVAL POSTGRADUATE SCHOOL Monterey, California



### **THESIS**

Theoretical Analysis of a Model for a Field Displacement Isolator

bу

Ram Sharon

June 1976

Thesis Advisor:

J. B. Knorr

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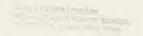
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#### ABSTRACT

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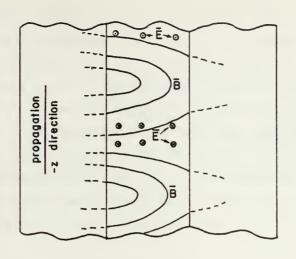
#### I. INTRODUCTION

The analysis of various configurations of microstrip transmission lines, is of great importance, primarily, to the industrial area, since these kinds of transmission lines are easy to manufacture, and they are suitable for use in microwave integrated circuits due to their small dimensions.

Two major groups of microstrip transmission lines can be defined, related to the substrate material that is used. These are the dielectric and ferrite substrate groups. This study presents the analysis of a new type of ferrite built, shielded microstrip isolator, using the edge-guided mode of propagation.

It was shown by M. E. Hines [Ref. 1] that an edge-guided mode of propagation occurs in a wide microstrip transmission line using a ferrite slab magnetized perpendicular to the ground plane. The R. F. fields patterns in such a structure are shown in Figure 1 [Ref. 1].

Propagation occurs in both  $\pm Z$  directions with equal phase velocities and loss, and the R. F. fields patterns are mirror images for both directions of propagation. In the dominant mode the energy is shifted from one side to the other with reversal of the direction of propagation. Hines suggested that this phenomenon could be used in the analysis of nonreciprocal devices such as isolators, phase shifters



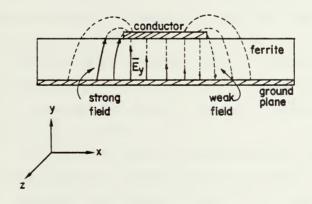


Figure 1. R.F. Fields of Dominant Mode in Microstrip Line. D.C. Magnetic Field in -y Direction.

and other components, where nonreciprocal behavior can be attained by perturbing the structure in an asymmetrical way.

To achieve isolation, a resistive load can be placed only on one side of the structure; thus high transmission loss occurs for the propagation direction for which the energy is concentrated on the lossy side, and lower loss results for the opposite direction where the energy is concentrated on the other side. The disadvantage of this field displacement isolator was the small ratio between backward and forward losses, which was not sufficient for isolation purposes.

An improved edge-guided mode isolator was suggested by K. Araki, T. Koyama and Y. Naito [Ref. 2] for which no lossy electric material was used, but instead one edge of the conducting strip was shorted to ground.

This isolation structure, shown in Figure 2, was built and tested and the experimental result showed large attenuation in the backward direction and small insertion loss in the forward direction.

The following study is an investigation of the theoretical behavior of a model for this isolator structure.

The exact configuration of the isolator model is shown in Figure 3. Since most of the field is confined in the dielectric substrate then the left, right and upper conducting walls of the shield have negligible affect on the electric and magnetic fields configuration, thus the model which is

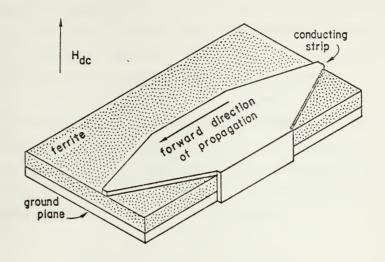


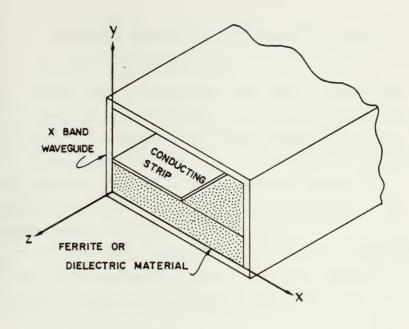
Figure 2. Isolator Structure.

easier to analyze can replace the open boundary-isolator configuration [Figure 2]. The shield is a rectangular wave-guide which implies that the highest frequency of operation should not exceed the cut-off frequency of the  ${\rm TE}_{10}$  mode of the waveguide.

The mathematical method which was selected for this study was used in earlier works like references 3, 4, and 5. This mathematical method can be used for calculating wavelength ratio and characteristic impedance for non TEM, TE or TM transmission lines. Essentially, this method deals with the boundary conditions of a structure, after they were transformed into the spectral domain. Then by using the

method of moment [Ref. 4] and assuming either current density distributions or electric field distributions (depending on the structure) numerical solutions for the wavelength ratio and the characteristic impedance can be obtained.

In essence, the analysis procedure is a complete solution for the dispersion characteristics of a structure built on a dielectric substrate, and then by applying perturbation theory, the phase and the attenuation constants of a structure built on a ferrite substrate are obtained. This ferrite built device is the isolator.



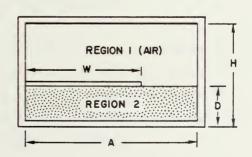


Figure 3. Three dimensional Isolator and Regions.

#### II. DISPERSION CHARACTERISTICS ON DIELECTRIC SUBSTRATE

#### A. FIELD AND BOUNDARY CONDITIONS

Assume waves are propagating along the structure shown in Figure 3, in the -Z direction such that the propagation term is  $e^{j\omega t + \gamma Z}$  where  $\omega$  is the radian frequency, and  $\gamma = \alpha + j\beta$  is the propagation constant. We assume from now on that for the dielectric substrate  $\gamma$  is pure imaginary, hence  $\alpha = 0$ . Later we shall see that for the ferrite subststrate,  $\gamma$  is a complex number including both terms  $\alpha$  and  $\beta$ .

The longitudinal components of the electric and magnetic fields can be expressed in terms of the scalar electric potential  $\phi^e$  and the scalar magnetic potential  $\phi^h$  as

$$Ez_{i} = Kc_{i}^{2} \phi_{i}^{e}(x,y)e^{\gamma Z}$$
 (1)

$$Hz_{i} = Kc_{i}^{2} \phi_{i}^{h}(x,y)e^{\gamma Z}$$
 (2)

where  $Kc_i^2 = K_i^2 + \gamma^2$  i = 1,2 defining the spatial regions of the structure (Figure 3). Using the two field expressions (1) and (2) together with Maxwell's curl equations leads to the transverse components of the electric and magnetic fields as follows:

$$Ex_{i} = \left(\gamma \frac{\partial \phi_{i}^{e}}{\partial x} - j\omega \mu_{i} \frac{\partial \phi_{i}^{h}}{\partial y}\right) e^{\gamma z}$$
 (3)

$$Hx_{i} = \left(\gamma \frac{\partial \phi_{i}^{h}}{\partial x} + j\omega \varepsilon_{i} \frac{\partial \phi_{i}^{e}}{\partial y}\right) e^{\gamma Z}$$
 (4)

$$Ey_{i} = \left(\gamma \frac{\partial \phi_{i}^{e}}{\partial y} + j\omega \mu_{i} \frac{\partial \phi_{i}^{h}}{\partial x}\right) e^{\gamma Z}$$
 (5)

$$Hy_{i} = \left(\gamma \frac{\partial \phi_{i}^{h}}{\partial y} - j\omega \varepsilon_{i} \frac{\partial \phi_{i}^{e}}{\partial x}\right) e^{\gamma z}$$
 (6)

$$i = 1, 2.$$

Applying boundary conditions at the interface between the dielectric substrate and the bottom wall of the waveguide (y=0), and assuming perfect conducting walls, tangential electric fields should be zero or explicitly writing

$$Ex_2(x,0,z) = 0$$
 (7)

$$Ez_2(x,0,z) = 0.$$
 (8)

At the interface between regions 1 and 2, (y=D) the tangential electric field must be continuous:

$$Ex_1(x,D,z) = Ex_2(x,D,z)$$
 (9)

$$Ez_1(x,D,z) = Ez_2(x,D,z).$$
 (10)

The electric fields at the interface between regions

l and 2 exist only in the dielectric portion of the interface
and can be written as:

$$Ex_{1}(x,D,z) = \begin{cases} 0 \text{ on strip} \\ e_{x}(x)e^{\gamma z} & W < X < A \end{cases}$$
 (11)

$$Ez_{1}(x,D,z) = \begin{cases} 0 \text{ on strip} \\ e_{z}(x)e^{\gamma z} & W < X < A. \end{cases}$$
 (12)

The tangential magnetic fields at the interface are discontinuous by the surface current densities, and assuming infinitessimally thin strip (can be considered as current sheet) the following boundary conditions can be written at y=D

$$Hx_{1}(x,D,z) - Hx_{2}(x,D,z) = \begin{cases} 0 & W < X < A \\ J_{z}(x)e^{\gamma z} & \text{on strip} \end{cases}$$
(13)

$$Hz_{1}(x,D,z) - Hz_{2}(x,D,z) = \begin{cases} 0 & W < X < A \\ Jx(x)e^{\gamma z} & \text{on strip.} \end{cases}$$

At the interface between region 1 and the upper wall of the waveguide (y=H) the tangential electric fields must be zero or explicitly writing

$$Ex_1(x,H,z) = 0$$
 (15)

$$Ez_1(x,H,z) = 0.$$
 (16)

Substituting the field expressions of equations (1) through (6) into the boundary condition expressions of equations (7) through (16) yields the following equations:

$$\gamma \frac{\partial \phi_2^{\mathbf{e}}(\mathbf{x}, 0)}{\partial \mathbf{x}} - j\omega \mu 2 \frac{\partial \phi_2^{\mathbf{h}}(\mathbf{x}, 0)}{\partial \mathbf{y}} = 0$$
 (17)

$$Kc_2^2 \phi_2^e(x,0) = 0$$
 (18)

$$\gamma \frac{\partial \phi_1^{e}(X,D)}{\partial x} - j\omega\mu_1 \frac{\partial \phi_1^{h}(X,D)}{\partial y} = \gamma \frac{\partial \phi_2^{e}(X,D)}{\partial x} - j\omega\mu_2 \frac{\partial \phi_2^{h}(X,D)}{\partial y}$$
(19)

$$Kc_1^2 \phi_1^e(X,D) = Kc_2^2 \phi_2^e(X,D)$$
 (20)

$$\gamma \frac{\partial \phi_1^{\mathbf{e}}(X,D)}{\partial x} - j\omega \mu_1 \frac{\partial \phi_1^{\mathbf{h}}(X,D)}{\partial y} = \begin{cases} 0 \text{ on strip} \\ ex(x) & W < X < A \end{cases}$$
 (21)

$$\operatorname{Kc}_{1}^{2} \phi_{1}^{e}(X,D) = \begin{cases} 0 \text{ on strip} \\ e_{7}(X) & W < X < A \end{cases}$$
 (22)

$$\gamma \frac{\partial \phi_1^h(X,D)}{\partial x} + j\omega \epsilon 1 \frac{\partial \phi_1^e(X,D)}{\partial y} -$$
 (23)

$$-\left(\gamma\frac{\partial\phi_{2}^{h}(X,D)}{\partial x}+j\omega\epsilon2\right.\frac{\partial\phi_{2}^{e}(X,D)}{\partial y})=\begin{cases}0&\text{W$$

$$Kc_{1}^{2} \phi_{1}^{h}(X,D) - Kc_{2}^{2} \phi_{2}^{h}(X,D) = \begin{cases} 0 & W < X < A \\ Jx(x) & \text{on strip} \end{cases}$$
 (24)

$$\gamma \frac{\partial \phi_1^{e}(X,H)}{\partial x} - j\omega \mu_1 \frac{\partial \phi_1^{h}(X,H)}{\partial y} = 0$$
 (25)

$$Kc_1^2 \phi_1^e(X,H) = 0.$$
 (26)

#### B. SPECTRAL DOMAIN TRANSFORM

The scalar potential functions  $\phi_i^e$  and  $\phi_i^h$  must satisfy Helmholtz's equations in the two spatial regions, thus

$$(\nabla_{xy}^{2} + Kc_{i}^{2}) \phi_{i}^{e}(x,y) = 0$$
 (27)

$$(\nabla_{xy}^{2} + Kc_{i}^{2}) \phi_{i}^{h}(x,y) = 0$$
 (28)

where  $Kc_i^2 = \gamma^2 + K_i^2 = K_i^2 - \beta^2$  and  $\nabla xy^2$  is a two-dimensional Laplacian operator.

As was suggested by Itoh and Mittra [Ref. 3] a Fourier transform was used in the  $\alpha$  domain. The transform is defined by:

$$F_{X}[\phi_{i}(x,y)] = \phi_{i}(\alpha,y) = \int_{-\infty}^{\infty} \phi_{i}(x,y) e^{j\alpha X} dx$$

$$i = 1,2.$$
(29)

Since the structure is closed boundary, a finite Fourier transform must be used instead of the infinite Fourier transform. The finite Fourier transform is given by

$$F_{X}[\phi_{i}(x,y)] = \phi_{i}(\alpha ny) = \int_{0}^{a} \phi_{i}e^{j\alpha nx} dx$$
 (30)

where  $\alpha n = \frac{2 \cdot \pi \cdot n}{A}$ 

and

$$F_{x}\left[\frac{\partial\phi_{i}(x,y)}{\partial x}\right] = -j\alpha n F_{x}\left[\phi_{i}(x,y)\right]. \tag{31}$$

By using equations (30) and (31), a general transform of equations (27) and (28) is given by

$$F_{x}\left[\frac{\partial \phi_{i}^{2}(x,y)}{\partial x^{2}}\right] + F_{x}\left[\frac{\partial \phi_{i}^{2}(x,y)}{\partial y^{2}}\right] + Kc_{i}^{2}F_{x}\left[\phi_{i}(x,y)\right] = 0$$
 (32)

Or explicitly writing:

$$\frac{\partial^2 \phi_i(\alpha n,y)}{\partial y^2} = \gamma_i^2 \phi_i(\alpha n,y)$$
 (33)

where  $\gamma_i^2 = \alpha_n^2 + \beta^2 - K_i^2$  i = 1,2.

Equation (33) should be analyzed for both regions 1 and 2, and the solutions will be the transforms of the electric and magnetic scalar potentials for both regions.

For region 1,

$$\gamma_1^2 = \alpha_n^2 + \beta^2 - K_1^2 \tag{34}$$

Where  $K_1 = \omega \overline{\epsilon_0 \mu_0} = \frac{2\pi}{\lambda o}$  and  $\beta = \frac{2\pi}{\lambda^+}$ .

Substituting  $K_1$  and  $\beta$  into equation (34) obtains,

$$\gamma_1^2 = \alpha_n^2 + (\frac{2\pi}{\lambda 0})^2 [(\frac{\lambda 0}{\lambda^T})^2 - 1].$$
 (35)

 $\lambda^{\prime}$  is the effective structure wavelength and is related to the free space wavelength  $\lambda$  by

$$\frac{\lambda O}{\sqrt{\epsilon r_1}} > \lambda' = \frac{\lambda O}{\sqrt{\epsilon r_{eff}}}$$
 (36)

where  $\epsilon r_{\mbox{eff}}$  is the effective relative dielectric constant of the device.

Since  $\epsilon_{r_1} = 1$  in region 1, equation (36) can be rewritten as

$$\lambda o > \lambda' = \frac{\lambda o}{\sqrt{\varepsilon_{reff}}} . \tag{37}$$

By using equation (37) together with equation (35) one can find that

$$\gamma_1^2 > \alpha_n^2 \tag{38}$$

Therefore  $\gamma_{\mbox{\scriptsize $1$}}$  is always a real quantity.

For region 2:

$$\gamma_2^2 = \alpha_n^2 + \beta^2 - K_2^2 \tag{39}$$

where  $K_2 = \omega \sqrt{\mu_2 \epsilon_2} = \frac{2\pi}{\lambda o} \sqrt{\mu_r 2 \epsilon_{r2}}$  .

By substituting  $K_2$  and  $\beta$  into equation (39) one can obtain

$$\gamma_2^2 = \alpha_n^2 - \left(\frac{2\pi}{\lambda_0}\right)^2 \left[\mu_{r_2} \epsilon_{r_2} = \left(\frac{\lambda_0}{\lambda^2}\right)^2\right]. \tag{40}$$

From equation (40) it is clear that  $\gamma_2$  can be either a real or an imaginary quantity, depending on the value of  $\alpha n$ .

 $\gamma_2$  will be imaginary for

$$-\frac{2\pi}{\lambda o}\sqrt{\left[\mu r_{2}\epsilon_{r_{2}}-\left(\frac{\lambda o}{\lambda^{\prime}}\right)^{2}\right]} < \alpha n < \frac{2\pi}{\lambda o}\sqrt{\left[\mu r_{2}\epsilon_{r_{2}}-\left(\frac{\lambda o}{\lambda^{\prime}}\right)^{2}\right]}$$
(41)

and will be real for

$$- \infty < \alpha n < -\frac{2\pi}{\lambda 0} \sqrt{\mu_{r_2} \epsilon_{r_2} - \left(\frac{\lambda 0}{\lambda^{1}}\right)^2}$$

$$\frac{2\pi}{\lambda 0} \sqrt{\mu_{r_2} \epsilon_{r_2} - \left(\frac{\lambda 0}{\lambda^{1}}\right)^2} < \alpha n < \infty . \tag{42}$$

The last two equations should be carefully observed while solving equation (33).

For region 1 equation (33) can be written as

$$\frac{\partial \phi_1^2(\alpha n, y)}{\partial y^2} = \gamma_1^2 \phi_1(\alpha n, y)$$
 (43)

and the solution has the form of

$$\Phi_{\uparrow}(\alpha n, y) = A(\alpha n) \cosh \gamma_{\uparrow} \cdot y + B(\alpha n) \sinh \gamma_{\uparrow} \cdot y$$
 (44)

For region 2, two solutions do exist corresponding to the real and imaginary values of  $\gamma_{2}\,.$ 

For Y2 real,

$$\Phi_2(\alpha n, y) = C(\alpha n) \cosh \gamma_2 y + D(\alpha n) \sinh \gamma_2 y$$
 (45)

and for  $\gamma_2$  imaginary

$$\Phi_2(\alpha n, y) = C(\alpha n) \cos \gamma_2 "y + jD(\alpha n) \sin \gamma_2 "y$$
 (46)

where  $\gamma_2 = j\gamma_2$ ".

After knowing the solutions for  $\phi_1(\alpha n,y)$  and  $\phi_2(\alpha n,y)$ , one can write the transforms of  $\phi_1^e$ ,  $\phi_2^e$ ,  $\phi_1^h$ ,  $\phi_2^h$  in both regions as follows.

#### Region 1 D<y<H

$$\phi_1^e(\alpha n, y) = A^e(\alpha n) \cosh \gamma_1(y-D) + B^e(\alpha n) \sinh \gamma_1(y-D)$$
 (47)

$$\phi_1^h(\alpha n, y) = A^h(\alpha n) \cosh_{\gamma_1}(y-D) + B^h(\alpha n) \sinh_{\gamma_1}(y-D)$$
 (48)

Region 2 0<y<D

$$\Phi_{2}^{e}(\alpha n,y) = \begin{cases} C_{H}^{e}(\alpha n) & \cosh_{2}y + D_{H}^{e}(\alpha n) & \sinh_{2}y , (\gamma_{2} \text{ real}) \end{cases} (49) \\ C_{T}^{e}(\alpha n) & \cos_{2}y + jD_{T}^{e}(\alpha n) & \sin_{2}y + (\gamma_{2} \text{ imaginary}) \end{cases} (50)$$

$$\Phi_{2}^{h}(\alpha n_{1}y) = \begin{cases} C_{H}^{h}(\alpha n) \cos h\gamma_{2}y + D_{H}^{h}(\alpha n) \sin h \gamma_{2}y, & (\gamma_{2} \text{ real}) \\ C_{T}^{h}(\alpha n) \cos \gamma_{2}^{"}y + jD_{T}^{h}(\alpha n) \sin \gamma_{2}^{"}y, & (\gamma_{2} \text{ imaginary}) \end{cases}$$

$$(51)$$

Superscript (e) indicates the electric field case and (h) indicates the magnetic field case.

All coefficients that appear in equations (47) through (52) can be determined by the boundary condition expressions. The above can be done by taking the Fourier transform of equations (17) through (26), substituting the field expressions for both cases of  $\gamma_2$ , real and imaginary, and finally solving for the coefficients.

The following equations are obtained:

### Hyperbolic Case $(\gamma_2 - real)$

$$-j\alpha n\gamma C_{H}^{e}(\alpha n) - j\omega \mu_{2} \gamma_{2} D_{H}^{h}(\alpha n) = 0$$
 (53)

$$\operatorname{Kc}_{2}^{2}\operatorname{C}_{H}^{e}(\alpha n) = 0 \tag{54}$$

$$Kc_1^2A^e(\alpha n) = E_z(\alpha n)$$
 (55)

$$-j\alpha n\gamma A^{e}(\alpha n) - j\omega \mu_{1}\gamma_{1}B_{H}^{h}(\alpha n) = E_{\chi}(\alpha n)$$
 (56)

$$\operatorname{Kc}_{1}^{2}\operatorname{A}^{h}(\alpha n) - \operatorname{Kc}_{2}^{2}\left[\operatorname{C}_{H}^{h}(\alpha n) \operatorname{cosh}_{2}\operatorname{D} + \operatorname{D}_{H}^{h}(\alpha n)\operatorname{sinh}_{2}\operatorname{D}\right] = J_{\nu}(\alpha n)$$
 (57)

$$-j\alpha n \gamma A^{h}(\alpha n) + j\omega \epsilon_{1} \gamma_{1} B^{e}(\alpha n) -$$
 (58)

- 
$$\{-j\alpha n\gamma[C_H^h(\alpha n)cosh\gamma_2D + D_H^h(\alpha n)sinh\gamma_2D] +$$

+ 
$$j\omega\epsilon_2[\gamma_2C_H^e(\alpha n)sinh\gamma_2D + \gamma_2D_H^e(\alpha n)cosh\gamma_2D]$$
} =  $J_z(\alpha n)$ 

$$\operatorname{Kc}_{1}^{2}\operatorname{A}^{e}(\alpha n) = \operatorname{Kc}_{2}^{2}[\operatorname{C}_{H}^{e}(\alpha n) \operatorname{cosh}_{2}\operatorname{D} + \operatorname{D}_{H}^{e}(\alpha n) \operatorname{sinh}_{2}\operatorname{D}]$$
 (59)

$$- j\alpha n\gamma A^{e}(\alpha n) - j\omega \mu_{1}\gamma_{1}B^{h}(\alpha) =$$
 (60)

- 
$$j\alpha n\gamma[C_H^e(\alpha n)cosh_{\gamma_2}D + D_H^e(\alpha n)sinh_{\gamma_2}D]$$
 -

- 
$$j_{\omega\mu_2\gamma_2}[C_H^h(\alpha n)sinh_{\gamma_2}D + D_H^h(\alpha n)cosh_{\gamma_2}D]$$

- 
$$j\alpha n\gamma[A^{e}(\alpha n)cosh\gamma_{1}(H-D) + B^{e}(\alpha n)sinh\gamma_{1}(H-D)]$$
 - (61)

$$- j_{\omega\mu_{1}\gamma_{1}}[A^{h}(\alpha n)sinh_{\gamma_{1}}(H-D) + B^{h}(\alpha n)cosh_{\gamma_{1}}(H-D)] = 0$$

$$Kc_1^2[A^e(\alpha n)cosh_{\gamma_1}(H-D) + B^e(\alpha)sinh_{\gamma_1}(H-D)] = 0.$$
 (62)

The coefficients for the hyperbolic case are obtained as follows:

$$C_{H}^{e}(\alpha n) = 0 \tag{63}$$

$$A^{e}(\alpha n) = \frac{E_{z}(\alpha n)}{Kc_{1}^{2}}$$
(64)

$$D_{H}^{h}(\alpha n) = 0 \tag{65}$$

$$B^{h}(\alpha n) = -\frac{\alpha n \gamma}{\omega \mu_{1} \gamma_{1} K c_{1}^{2}} E_{z}(\alpha n) + j \frac{1}{\omega \mu_{1} \gamma_{1}} E_{x}(\alpha n)$$
 (66)

$$D_{H}^{e}(\alpha n) = \frac{1}{Kc_{2}^{2} \sinh_{\gamma_{2}} D} E_{Z}(\alpha n)$$
 (67)

$$C_{H}^{h}(\alpha n) = -\frac{\alpha n \gamma}{K c_{2}^{2} \omega \mu_{2} \gamma_{2} sinh \gamma_{2} D} E_{z}(\alpha n) + j \frac{1}{\omega \mu_{2} \gamma_{2} sinh \gamma_{2} D} E_{x}(\alpha n)$$
(68)

$$B^{e}(\alpha n) = -\frac{\operatorname{ctgh}_{\gamma_{1}}(H-D)}{\operatorname{Kc}_{1}^{2}} E_{z}(\alpha n)$$
 (69)

$$A^{h}(\alpha n) = \frac{\alpha n \cdot \gamma \cdot \operatorname{ctgh}_{\gamma_{1}}(H-D)}{\omega \mu_{1} \gamma_{1} K c_{1}^{2}} E_{z}(\alpha n) - j \frac{\operatorname{ctgh}_{\gamma_{1}}(H-D)}{\omega \mu_{1} \gamma_{1}} E_{x}(\alpha n)$$
 (70)

When substituting equation (63) through (70) into equations (57) and (58) one can form two sets of equations

$$F_1^{H}(\alpha n,\beta) E_X(\alpha n) + F_2^{H}(\alpha n,\beta) E_Z(\alpha n) = J_X(\alpha n)$$
 (71)

$$F_{3}^{H}(\alpha n,\beta)E_{x}(\alpha n) + F_{4}^{H}(\alpha n,\beta)E_{z}(\alpha n) = J_{z}(\alpha n)$$
 (72)

or in matrix form

$$\begin{bmatrix} F_1^{H}(\alpha n, \beta) & F_2^{H}(\alpha n, \beta) \\ F_3^{H}(\alpha n, \beta) & F_4^{H}(\alpha n, \beta) \end{bmatrix} \begin{bmatrix} E_{\chi}(\alpha n) \\ E_{Z}(\alpha n) \end{bmatrix} = \begin{bmatrix} J_{\chi}(\alpha n) \\ J_{Z}(\alpha n) \end{bmatrix}$$
(73)

where  $\gamma = j\beta$ .

The elements of the matrix  $[F^H]$  are given as follows:

$$F_1^{H}(\alpha n,\beta) = -j \left[ \frac{Kc_1^2 ctgh_{\Upsilon_1}(H-D)}{\omega \mu_1 \gamma_1} + \frac{Kc_2^2 ctgh_{\Upsilon_2}D}{\omega \mu_2 \gamma_2} \right]$$
(74)

$$F_{2}^{H}(\alpha n,\beta) = j \left[ \frac{\alpha n\beta \operatorname{ctgh}_{\gamma_{1}}(H-D)}{\omega \mu_{1}\gamma_{1}} + \frac{\alpha_{n}\beta \operatorname{ctgh}_{\gamma_{2}}D}{\omega \mu_{2}\gamma_{2}} \right]$$
(75)

$$F_3^{H}(\alpha n,\beta) = -F_2^{H}(\alpha n,\beta) \tag{76}$$

$$F_{4}^{H}(\alpha n,\beta) = j \left[ \frac{(\alpha n\beta)^{2} \operatorname{ctgh}_{\gamma_{1}}(H-D)}{\omega \mu_{1} \gamma_{1} K c_{1}^{2}} - \frac{\omega \varepsilon_{1} \gamma_{1} \operatorname{ctgh}_{\gamma_{1}}(H-D)}{K c_{1}^{2}} - \frac{(77)}{\kappa c_{1}^{2}} - \frac{\omega \varepsilon_{2} \gamma_{2} \operatorname{ctgh}_{\gamma_{2}}D}{\kappa c_{2}^{2}} + \frac{(\alpha n\beta)^{2} \operatorname{ctgh}_{\gamma_{2}}D}{\kappa c_{2}^{2} \omega \mu_{2} \gamma_{2}} \right].$$

The same method can be applied to the  $\frac{trigonometric\ case}{(\gamma_2)}$  imaginary) and the following equations are obtained:

$$C_{T}^{e}(\alpha n) = 0 \tag{78}$$

$$D_{\mathsf{T}}^{\mathsf{h}}(\alpha \mathsf{n}) = 0 \tag{79}$$

$$D_{T}^{e}(\alpha n) = -j \frac{1}{Kc_{2}^{2} \sin \gamma_{2}"D} E_{Z}(\alpha n)$$
(80)

$$C_{T}^{h}(\alpha n) = \frac{\alpha n \gamma}{K c_{2}^{2} \omega \mu_{2} \gamma_{2}^{"} \sin \gamma_{2}^{"} D} E_{z}(\alpha n) - j \frac{1}{\omega \mu_{2} \gamma_{2}^{"} \sin \gamma_{2}^{"} D} E_{x}(\alpha n)$$
(81)

$$\operatorname{Kc}_{1}^{2} \operatorname{A}^{h}(\alpha n) - \operatorname{Kc}_{2}^{2} \left[\operatorname{C}_{T}^{h}(\alpha n) \operatorname{cos}_{Y_{2}}^{u} + \operatorname{jD}_{T}^{h}(\alpha n) \operatorname{sin}_{Y_{2}}^{u} \right] =$$

$$= J_{v}(\alpha n) \tag{82}$$

$$-j\alpha n_{\Upsilon}A^{h}(\alpha n) + j\omega \varepsilon_{1}\gamma_{1}B^{e}(\alpha n) - j\alpha n_{\Upsilon}C^{h}_{T}(\alpha n)\cos \gamma_{2}"D +$$

$$+ \omega \varepsilon_{2}\gamma_{2}"D^{e}_{T}(\alpha n)\cos \gamma_{2}"D = J_{z}(\alpha n) . \tag{83}$$

When substituting equations (69), (70) and (78) through (81) into equations (82) and (83) one can obtain the matrix form

$$\begin{bmatrix} F_1^{\mathsf{T}}(\alpha n, \beta) & F_2^{\mathsf{T}}(\alpha n, \beta) \\ F_3^{\mathsf{T}}(\alpha n, \beta) & F_4^{\mathsf{T}}(\alpha n, \beta) \end{bmatrix} \begin{bmatrix} E_{\mathsf{X}}(\alpha n) \\ E_{\mathsf{Z}}(\alpha n) \end{bmatrix} = \begin{bmatrix} J_{\mathsf{X}}(\alpha n) \\ J_{\mathsf{Z}}(\alpha n) \end{bmatrix}$$
(84)

where again  $\gamma = j\beta$ 

and the elements of the matrix  $[F^T]$  are given as follows:

$$F_1^T(\alpha n, \beta) = -j \left[ \frac{Kc_1^2 ctgh_{\Upsilon_1}(H-D)}{\omega \mu_1 \Upsilon_1} - \frac{Kc_2^2 ctg_{\Upsilon_2}^{"D}}{\omega \mu_2 \Upsilon_2^{"}} \right]$$
 (85)

$$F_2^{\mathsf{T}}(\alpha n,\beta) = j \left[ \frac{\alpha n\beta \operatorname{ctgh}_{\gamma_1}(\mathsf{H}-\mathsf{D})}{\omega \mu_1 \gamma_1} - \frac{\alpha n\beta \operatorname{ctg}_{\gamma_2} \mathsf{D}}{\omega \mu_2 \gamma_2} \right]$$
(86)

$$F_3^{T}(\alpha n,\beta) = -F_2^{T}(\alpha n,\beta)$$
 (87)

$$F_{4}^{T}(\alpha n,\beta) = j \left[ \frac{(\alpha n\beta)^{2} \operatorname{ctgh}_{Y_{1}}(H-D)}{\omega \mu_{1} Y_{1} K c_{1}^{2}} - \frac{\omega \varepsilon_{1} Y_{1} \operatorname{ctgh}_{Y_{1}}(H-D)}{K c_{1}^{2}} - \frac{(\alpha n\beta)^{2} \operatorname{ctg}_{Y_{2}}"D}{K c_{2}^{2} \omega \mu_{2} Y_{2}"} - \frac{\omega \varepsilon_{2} Y_{2}" \operatorname{ctg}_{Y_{2}}"D}{K c_{2}^{2}} \right].$$
(88)

Expressions (73) and (84) can be written in a general form as

$$\begin{bmatrix} F_1^{H,T}(\alpha n,\beta) & F_2^{H,T}(\alpha n,\beta) \\ F_3^{H,T}(\alpha n,\beta) & F_4^{H,T}(\alpha n,\beta) \end{bmatrix} \begin{bmatrix} E_{\chi}(\alpha n) \\ E_{z}(\alpha n) \end{bmatrix} = \begin{bmatrix} J_{\chi}(\alpha n) \\ J_{z}(\alpha n) \end{bmatrix}$$
(89)

from which solutions to  $E_{\chi}(\alpha n)$  and  $E_{Z}(\alpha n)$  in terms of  $J_{\chi}(\alpha n)$  and  $J_{\chi}(\alpha n)$  can be obtained as follows:

$$\mathcal{E}_{\chi}(\alpha n) = \frac{J_{\chi}(\alpha n)F_{4}^{H,T}(\alpha n,\beta) - J_{z}(\alpha n)F_{2}^{H,T}(\alpha n,\beta)}{F_{1}^{H,T}(\alpha n,\beta) \cdot F_{4}^{H,T}(\alpha n,\beta) - F_{2}^{H,T}(\alpha n,\beta) \cdot F_{3}^{H,T}(\alpha n,\beta)}$$

$$E_{z}(\alpha n) = \frac{J_{x}(\alpha n)F_{3}^{H,T}(\alpha n,\beta) + J_{z}(\alpha n)\cdot F_{1}^{H,T}(\alpha n,\beta)}{F_{1}^{H,T}(\alpha n,\beta) + F_{4}^{H,T}(\alpha n,\beta) - F_{2}^{H,T}(\alpha n,\beta)\cdot F_{3}^{H,T}(\alpha n,\beta)}$$
(91)

Define the following terms

$$DN = F_1^{H,T}(\alpha n,\beta) F_4^{H,T}(\alpha n,\beta) - F_2^{H,T}(\alpha n,\beta) F_3^{H,T}(\alpha n,\beta)$$
 (92)

$$M_{1(\alpha n,\beta)}^{H,T} = \frac{F_{4(\alpha n,\beta)}^{H,T}}{DN}$$
(93)

$$M_{2(\alpha n,\beta)}^{H,T} = -\frac{F_{2(\alpha n,\beta)}^{H,T}}{DN}$$
(94)

$$M_{3(\alpha n,\beta)}^{H,T} = -\frac{F_{3(\alpha n,\beta)}^{H,T}}{DN} = -M_{2}^{H,T}(\alpha n,\beta)$$
 (95)

$$M_{4(\alpha n,\beta)}^{H,T} = \frac{F_1^{H,T}(\alpha n,\beta)}{DN}$$
(96)

which lead to the final expressions

$$E_{\chi}(\alpha n) = M_1^{H,T}(\alpha n,\beta) J_{\chi}(\alpha n) + M_2^{H,T}(\alpha n,\beta) J_{\chi}(\alpha n)$$
 (97)

$$E_{z}(\alpha n) = M_{3}^{H,T}(\alpha n,\beta) J_{x}(\alpha n) + M_{4}^{H,T}(\alpha n,\beta) J_{z}(\alpha n) . \qquad (98)$$

#### C. DETERMINENTAL EQUATION

Nothing seems to be gained so far since neither the electric field and the current density components nor their transforms are known. In order to simplify equation (97) and (98), the method of moments [Ref. 4] is applied in the spectral domain. Define a scalar product over the domain  $-\infty < \alpha n < \infty$  according to reference 6 as

$$\langle a(\alpha n), b(\alpha n) \rangle = \sum_{n=-\infty}^{n=\infty} a(\alpha n) \cdot b^*(\alpha n).$$
 (99)

Thus when applying this concept to equation (95) and (96) and choosing  $a(\alpha n) = \mathcal{E}_X(\alpha n)$  or  $\mathcal{J}_Z(\alpha n)$  and  $b(\alpha n) = \mathcal{J}_X(\alpha n)$  or  $\mathcal{J}_Z(\alpha n)$  respectively, one can obtain

$$\langle M_1^{H,T}(\alpha n,\beta) J_X(\alpha n), J_X(\alpha n) \rangle + \langle M_2^{H,T}(\alpha n,\beta) J_Z(\alpha n), J_X(\alpha n) \rangle = 0$$

$$(100)$$

$$+  = 0.$$
(101)

By using Parseval's theorem it can easily be shown that the right hand side of the above two equations is equal to zero, due to the orthogonality of  $E_{\rm Z}(\alpha n)$  and  $J_{\rm Z}(\alpha n)$ , and  $E_{\rm X}(\alpha n)$  and  $J_{\rm X}(\alpha n)$ .

In general, one can expand each current density component in a set of basis functions such as:

$$J_{z}(x) = \sum_{k=1}^{\infty} a_{1k} f_{zk}(x)$$
 (102)

$$J_{X}(x) = \sum_{k=1}^{\infty} a_{2k} g_{zk}'(x) . \qquad (103)$$

In the following analysis, one term approximation is used since it was found to be less complicated, without much degradation in the accuracy of the final results.

So with

$$J_{z}(\alpha n) \approx F\{al \cdot f_{z}(x)\} = a_{l}f_{z}(\alpha n)$$
 (104)

and

$$J_{X}(\alpha n) \approx F\{a_{2} \cdot g_{X}'(x)\} = a_{2} \cdot g_{X}(\alpha n)$$
 (105)

equations (100) and (101) become

$$a_{2} \sum_{n=-\infty}^{\infty} M_{1}^{H,T}(\alpha n,\beta) |g_{X}(\alpha n)|^{2} + a_{1} \sum_{n=-\infty}^{\infty} M_{2}^{H,T}(\alpha n,\beta)$$

$$f_{Z}(\alpha n) g_{X}^{*}(\alpha n) = 0$$
(106)

$$a_{2} \sum_{n=-\infty}^{\infty} M_{3}^{H,T}(\alpha n,\beta) g_{X}(\alpha n) f_{Z}^{*}(\alpha n) + a_{1} \sum_{n=-\infty}^{\infty} M_{4}^{H,T}(\alpha n,\beta),$$

$$(107)$$

From the geometry of the device (Fig. 3) and the location of the coordinate system it is clear that all choices of current density distributions,  $J_z(x)$  and  $J_x(x)$ , are neither even nor odd functions.

Each current density distribution can be expressed as a linear function of even and odd functions as follows:

$$J_{z}(x) = a_{1}[f'_{ze}(x) + f'_{zo}(x)]$$
 (108)

$$J_{x}(x) = a_{2}[g'_{xe}(x) + g'_{xo}(x)]$$
 (109)

When taking the Fourier transform of equations (108) and (109) then according to reference 7, the following transforms are obtained

$$J_{z}(\alpha n) = a_{\uparrow}[f_{ze}(\alpha n) + jf_{zo}(\alpha n)] = a_{\uparrow}f_{z}(\alpha n)$$
 (110)

$$J_{x}(\alpha n) = a_{2}[g_{xe}(\alpha n) + jg_{xo}(\alpha n)] = a_{2}g_{x}(\alpha n).$$
 (111)

In order to solve equations (106) and (107) for the non-trivial solution, the determinant of the coefficient matrix should be set to zero for all sets of physical parameters, at each frequency of operation. The above can be

achieved by finding the appropriate  $\beta$  that satisfies this requirement. From that  $\beta$  the dispersion characteristics of the device can be calculated.

The determinental equation has the form of

$$\left[\sum_{n=-\infty}^{\infty} M_{1}^{H,T}(\alpha n,\beta) |g_{X}(\alpha n)|^{2}\right] \cdot \left[\sum_{n=-\infty}^{\infty} M_{4}^{H,T}(\alpha n,\beta) |f_{Z}(\alpha n)|^{2}\right] - \left[\sum_{n=-\infty}^{\infty} M_{2}^{H,T}(\alpha n,\beta) \cdot f_{Z}(\alpha n) |g_{X}^{*}(\alpha n)\right] \cdot \left[\sum_{n=-\infty}^{\infty} M_{3}^{H,T}(\alpha n,\beta) - g_{X}^{*}(\alpha n)\right] = 0$$

$$\left[g_{X}(\alpha n) f_{Z}^{*}(\alpha n)\right] = 0$$
(112)

By investigating equations (93) through (96) one may observe that  $M_1(\alpha n,\beta)$  and  $M_4(\alpha n,\beta)$  are even functions, while  $M_2(\alpha n,\beta)$  and  $M_3(\alpha n,\beta)$  are odd functions.

Using this information together with equations (110) and (111) leads to the final expression of the determinental equation

$$\left[\sum_{n=-\infty}^{\infty} M_{1}^{H,T}(\alpha n,\beta) |g_{X}(\alpha n)|^{2}\right] \cdot \left[\sum_{n=-\infty}^{\infty} M_{4}^{H,T}(\alpha n,\beta) |f_{Z}(\alpha n)|^{2}\right] + \left[\sum_{n=-\infty}^{\infty} M_{2}^{H,T}(\alpha n,\beta) \cdot B(\alpha n)\right]^{2} = 0$$
(113)

where

$$B(\alpha n) = -f_{ze}(\alpha n) \cdot g_{xo}(\alpha n) + f_{zo}(\alpha n) \cdot g_{xe}(\alpha n). \quad (114)$$

In addition to the requirement that the determinant of the coefficients matrix should be set to zero, one can see from equations (106), (113) and (114) that the ratio of the two coefficients has the form of

$$\frac{a_1}{a_2} = j \left[ \sum_{n=-\infty}^{\infty} M_1^{H,T}(\alpha n,\beta) |g_{\chi}(\alpha n)|^2 \right]$$

$$\sum_{n=-\infty}^{\infty} M_2^{H,T}(\alpha n,\beta) B(\alpha n)$$
(115)

Since the expression in the brackets is a real quantity, it is well understood that there is a 90° phase difference (in time) between the two current density components.

#### D. CURRENT DENSITY COMPONENTS

After the determinental equation was simplified as shown in equation (113), the two current density components  $J_z(x)$  and  $J_x(x)$  were approximated, thus that the equation could have been solved. Various one term approximations were investigated and the set of components that was chosen to be substituted in the determinental equation was the one found as the best approximation of both current distribution components.

The approximated current density component in the z-direction has the form

$$J_{z}(x) = \begin{cases} a_{1}e^{20\frac{X}{W}} & \text{on the strip} \\ 0 & \text{elsewhere} \end{cases}$$
 (116)

and in the x-direction

$$J_{X}(x) = \begin{cases} a_{2} \cos \frac{\pi x}{2W} & \text{on the strip} \\ 0 & \text{elsewhere} \end{cases}$$
 (117)

The two current density components are shown in Figure 4.

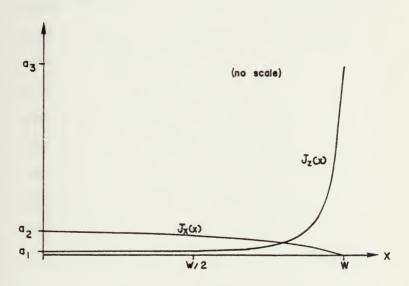


Figure 4. Longitudinal and Transverse Current Density Components.

It is clear that the ratio  $a_3/a_1=e^{20}=4.85\cdot 10^8$  indicates that most of the current that flows in the z-direction is concentrated at the right edge of the strip [Fig. 3]. On the other hand the choice of  $J_X(x)$  indicates that there is no current in the x-direction at the right-edge of the strip.

Computer output indicated a frequency dependent of the ratio  $a_3/a_2$  as shown in Figure 5. This curve was plotted for D = 0.125" w = 0.45"  $\epsilon_r$  = 16 and  $a_1$  =  $10^{-10}$ .

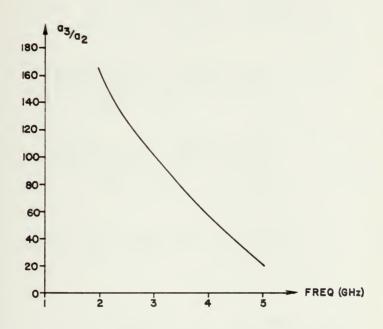


Figure 5. Ratio of the Maximum Current Density Components

From Figure 5 one may learn that the transverse current component on the strip increases relative to the longitudinal component, as the frequency increases.

The Fourier transforms of the current density components are given as:

$$J_{z}(\alpha n) = \int_{0}^{w} a_{1}e^{20\frac{x}{w}} e^{j\alpha nx} dx = a_{1} \cdot f_{z}(\alpha n) =$$
 (118)

$$= a_{1} \left[ \frac{\frac{20}{w} (e^{20} \cos \alpha nw - 1) + e^{20} \cdot \alpha n \cdot \sin \alpha nw}{(\frac{20}{w})^{2} + (\alpha n)^{2}} + \right]$$

+ j 
$$\frac{-\alpha n(e^{20}\cos\alpha nw-1) + \frac{20}{w}e^{20}\sin\alpha nw}{(\frac{20}{w})^2 + (\alpha n)^2}$$

$$J_{\chi}(\alpha n) = \int_{0}^{W} a_{2} \cos \frac{\pi x}{2w} e^{j\alpha nw} = a_{2} g_{\chi}(\alpha n) =$$
 (119)

$$= a_2 \left[ \frac{\frac{\pi}{2w} \cos \alpha nw}{\left(\frac{\pi}{2w}\right)^2 - (\alpha n)} + j \frac{\frac{\pi}{2w} \sin \alpha nw + \alpha n}{\left(\frac{\pi}{2w}\right)^2 - (\alpha n)} \right]$$

where the even and odd components of each transform can be identified by refering to equations (110) and (111).

After substituting equations (118) and (119) into equation (113), the determinental equation was programmed into Fortran language and the root  $\beta$  that set the determinental

equation equal to zero, was found by an iteration method on a digital computer. From the value of  $\beta,~\lambda'/\lambda$  could easily be calculated.

# Figure 6 shows:

- 1. Computed and measured  $\lambda'/\lambda$  vs. frequency for D = 0.125", W = 0.45",  $\epsilon_r$  = 16.
- 2. Computed  $\lambda'/\lambda$  vs. frequency for D = 0.025", w = 0.45",  $\epsilon_{\gamma}$  = 16.

Both curves are plotted for A = 0.9", H = 0.4".

It can be seen that there is a good agreement between experimental and computed wavelength ratio. The highest deviation is on the order of 10 percent which can be attributed largely to the experimental apparatus.

One can learn that the wavelength's ratio is directly proportional to the dielectric substrate width, which implies that the fields are more confined in the dielectric substrate as its width decreases.

#### E. AVERAGE POWER FLOW

For later discussion of the characteristics of the device built on ferrite substrate, a perturbation technique is used.

One of the entries to the perturbation expression is the average power flow in the device built on a dielectric substrate.

A general expression for the time average power flow in the direction of propagation is given by

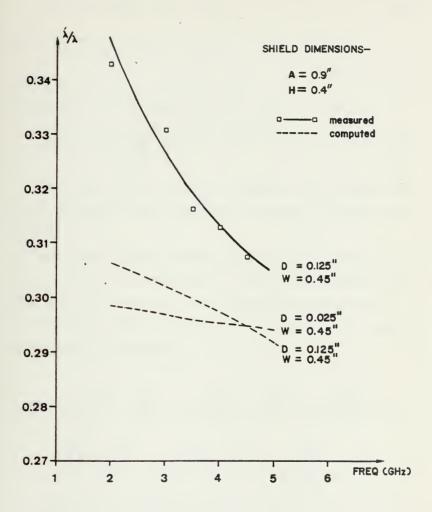


Figure 6. Computed and Measured Dispersion Characteristics for D = 0.025" W = 0.45" and D = 0.125" W = 0.45" with  $\epsilon_{r}$  = 16.

Pave = 
$$\frac{1}{2} \operatorname{Re} \iint_{S} (\bar{E} x \bar{H}^*) \cdot \hat{a}_{z} da$$
 (120)

Since 
$$(ExH^*) \cdot \hat{a}_z = ExHy^* - EyHx^*$$

and da = dx dy

then equation (120) can be rewritten as

Pave = 
$$-\frac{1}{2}$$
 Re  $\iint_S$  (ExHy\* - EyHx\*) dx dy (121)

The minus sign was added in equation (121) to make the result positive (recall propagation in the -z direction was assumed).

Both the electric and the magnetic fields are known in terms of the scalar potentials  $\phi^e$  and  $\phi^h$  thus substituting equations (3) through (6) into equation (121) and using  $\gamma=j\beta$  for the waves traveling in the -z direction, leads to the following expression

$$P_{\hat{i}} \text{ ave } = -\frac{1}{2} \text{Re} \left\{ \iint_{S} (j\beta \frac{\partial \phi_{\hat{i}}^{e}}{\partial x} - j\omega \mu_{\hat{i}} \frac{\partial \phi_{\hat{i}}^{h}}{\partial y}) (-j\beta \frac{\partial \phi_{\hat{i}}^{h}}{\partial y} + j\omega \epsilon_{\hat{i}} \frac{\partial \phi_{\hat{i}}^{e}}{\partial x}) dx dy + \iint_{S} (j\beta \frac{\partial \phi_{\hat{i}}^{e}}{\partial y} + j\omega \mu_{\hat{i}} \frac{\partial \phi_{\hat{i}}^{h}}{\partial x}) (j\beta \frac{\partial \phi_{\hat{i}}^{h}}{\partial x} + j\omega \epsilon_{\hat{i}} \frac{\partial \phi_{\hat{i}}^{e}}{\partial y}) dx dy \right\}$$

$$= 1, 2$$

Subscript i denotes the spatial regions, air and dielectric substrate respectively, for which equation (122) must be evaluated.

The total average power flow in the device is the sum of the spatial power components that flow both in the air and in the dielectric substrate as shown in the following equation

$$Pave_{ToT} = P_1 ave + P_2 ave$$
 (123)

Applying Parseval's theorem to equation (122) obtains

$$P_{i} \text{ ave } = -\frac{1}{2A} \text{ Re } \sum_{n=-\infty}^{\infty} \left\{ -\alpha n^{2} \omega \beta \epsilon_{i} | \Phi_{i}^{e}(\alpha n, y)|^{2} - (124) \right\}$$

$$-\alpha n^{2} \omega \beta \mu_{i} | \Phi_{i}^{h}(\alpha n, \beta)|^{2} - \omega \beta \mu_{i} | \frac{\partial \Phi_{i}^{h}(\alpha n, y)}{\partial y}|^{2} - (124)$$

$$-\omega \beta \epsilon_{i} | \frac{\partial \Phi_{i}^{e}(\alpha n, y)}{\partial y}|^{2} - j \alpha n \beta^{2} \left[ \Phi_{i}^{e}(\alpha n, y) \frac{\partial \Phi_{i}^{h*}(\alpha n, y)}{\partial y} + \Phi_{i}^{h*} \frac{\partial \Phi_{i}^{e}(\alpha n, y)}{\partial y} \right] + j \alpha n K_{i}^{2} \left[ \Phi_{i}^{e*} \frac{\partial \Phi_{i}^{h}(\alpha n, y)}{\partial y} + \Phi_{i}^{h*} \frac{\partial \Phi_{i}^{e*}(\alpha n, y)}{\partial y} \right] \right\} dy$$

The limits of integration depend on each region and are  $\int_{0}^{H}$  for region 1 and  $\int_{0}^{D}$  for region 2.

After obtaining the general expression for average power flow, one can apply it for both regions.

Recall equations (47), (48), (64), (66), (69) and (70) and have the first two modified, the following equations can be obtained

$$\Phi_{\uparrow}^{e}(\alpha n, y) = A(\alpha n) \sin h_{\Upsilon_{\uparrow}}(y-H)$$
 (125)

$$\Phi_{1}^{h}(\alpha n, y) = A(\alpha n) \cos h_{Y_{1}}(y-H)$$
 (126)

where

$$A^{-e}(\alpha n) = \frac{E_z(\alpha n)}{Kc_1^2 \sin h\gamma_1(D-H)}$$
 (127)

$$A^{-h}(\alpha n) = -j \left[ \frac{\alpha n \beta \mathcal{E}_{z}(\alpha n)}{K c_{1}^{2}} - \mathcal{E}_{x}(\alpha n) \right] \frac{1}{\omega \mu_{1} \gamma_{1} \sin h \gamma_{1}(D-H)}$$
(128)

After using the modified expressions for  $\Phi_1^e(\alpha n,y)$  and  $\Phi_1^h(\alpha n,y)$  in region 1, and integrating with respect to y, one can obtain

$$P_{1}ave = \frac{1}{4A} Re \sum_{n=-\infty}^{\infty} \left\{ \omega_{\beta} \left[ \frac{\sin h 2\gamma_{1}(H-D)}{2\gamma_{1}} - \frac{1}{2} (H-D) \right] - \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} \right) \right] + \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} \right) \right) \left[ \frac{1}{2} - \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} \right) \right] + \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} - \frac{1}{2} \left( \frac{1}{2} - \frac{1}{2} - \frac{1}{2} - \frac{1}{2} \right) \right] + \frac{1}{2} \left( \frac{1}{2} - \frac{1}{$$

In region 2, there are two expressions depending upon whether  $\gamma_2$  is a real or imaginary quantity. As in region 1, the integration with respect to y can be done analytically, and the following equations are obtained.

For  $\gamma_2$  real,

$$\begin{split} & P_{2} a v e_{H} = \frac{1}{4A} \ \text{Re} \ \sum_{n=-\infty}^{\infty} \left\{ \omega \beta \left[ \alpha n^{2} \epsilon_{2} | D_{H}^{e}(\alpha n) |^{2} + \right. \right. \\ & + \left. \gamma_{2}^{2} \mu_{2} | C_{H}^{h}(\alpha n) |^{2} \right] \left[ \frac{\sin h 2 \gamma_{2} D}{2 \gamma_{2}} - D \right] + \left. \omega \beta \left[ \alpha n^{2} \mu_{2} | C_{H}^{h}(\alpha n) |^{2} + \right. \\ & + \left. \gamma_{2}^{2} \epsilon_{2} | D_{H}^{e}(\alpha n) |^{2} \right] \left[ \frac{\sin h 2 \gamma_{2} D}{2 \gamma_{2}} + D \right] + \left. j \alpha n \left[ \beta^{2} D_{H}^{e}(\alpha n) C_{H}^{h*}(\alpha n) - \right. \\ & - \left. K_{2}^{2} D_{H}^{e*}(\alpha n) C_{H}^{h}(\alpha n) \right] \sin h \ 2 \gamma_{2} D \right\} \end{split}$$

and for  $\gamma_2$  imaginary,  $(\gamma_2 = j\gamma_2")$ 

$$P_{2}ave_{T} = \frac{1}{4A} Re \sum_{n=-\infty}^{\infty} \left\{ \omega_{\beta} \left[ \alpha_{n}^{2} \epsilon_{2} | D_{T}^{e}|^{2} + \gamma_{2}^{"2} \mu_{2} | C_{T}^{h}|^{2} \right] \right\}. \quad (131)$$

$$\cdot \left[ D - \frac{\sin_{2} \gamma_{2}^{"D}}{2 \gamma_{2}^{"}} \right] + \omega_{\beta} \left[ \alpha_{n}^{2} \mu_{2} | C_{T}^{h}|^{2} + \gamma_{2}^{"2} \epsilon_{2} | D_{T}^{e}|^{2} \right] \left[ D + \frac{\sin_{2} \gamma_{2}^{"D}}{2 \gamma_{2}^{"}} \right] + \gamma_{2}^{"2} \epsilon_{2} | D_{T}^{e}|^{2} \left[ D_{T}^{e} + K_{2}^{2} C_{T}^{h} D_{T}^{e} \right] \sin_{2} \gamma_{2}^{"D} \right\}$$

 $D_H^e(\alpha n)$ ,  $C_H^h(\alpha n)$ ,  $D_T^e(\alpha n)$  and  $C_T^h(\alpha n)$  are given in equation (67), (68), (80) and (81) respectively

The total power in region 2 becomes

$$P_2^{ave} = P_2^{ave} + P_2^{ave}$$
 (132).

Detailed development of equations (129) through (131) is given in appendix A.

Curves of  $\alpha$ -domain power distributions for regions 1 and 2 are shown in Figures 7 and 8 respectively. The ratio of the power carried in each region to the total power carried in the device for various parameters, is plotted as a function of frequency in Figures 9 and 10.

Several facts can be studied from the graphs.

- (a) The amount of power carried in each region is frequency dependent.
- (b) As frequency increases relatively more power is carried through region 2, the dielectric substrate.
- (c) Relatively more power is carried through region 1 as the permittivity is lowered.
- (d) In the low frequency region, more power is carried through region 1 as the substrate thickness increases. At high frequencies the power carried in region 1 approaches the same value, for all values of substrate thickness.
- (e) As strip width increases more power is carried through region 2, the dielectric substrate,

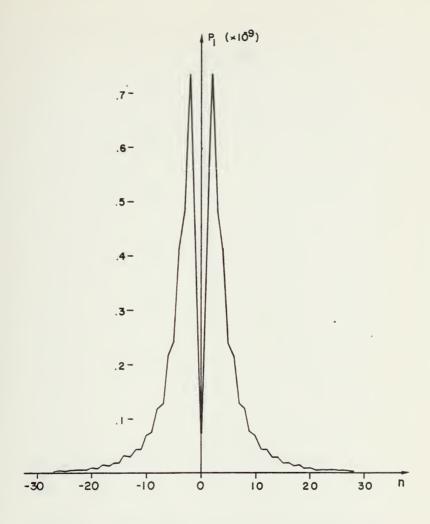


Figure 7. Average Power Distribution in Region 1 Vs. n (an) for f = 4GHz, D = 0.125", M = 0.45",  $\epsilon_{\rm r}$  = 16.

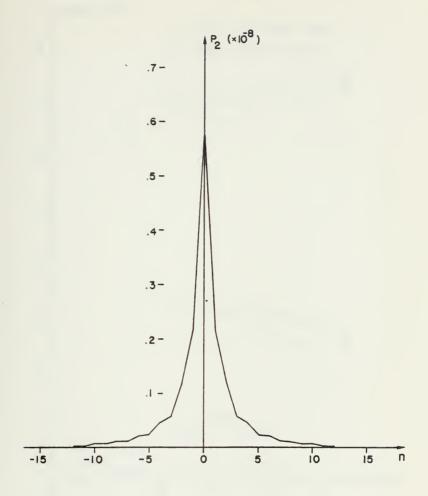


Figure 8. Average Power Distribution in Region 2 Vs. n ( $\alpha$ n) for f = 4GHz, D = 0.125", W = 0.45",  $\epsilon_r$  = 16.

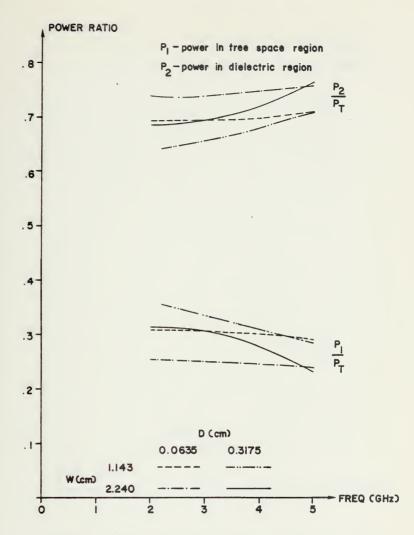


Figure 9. Average Power Ratio in Regions 1 and 2 Vs. Frequency for  $\epsilon_{\rm r}$  = 9.

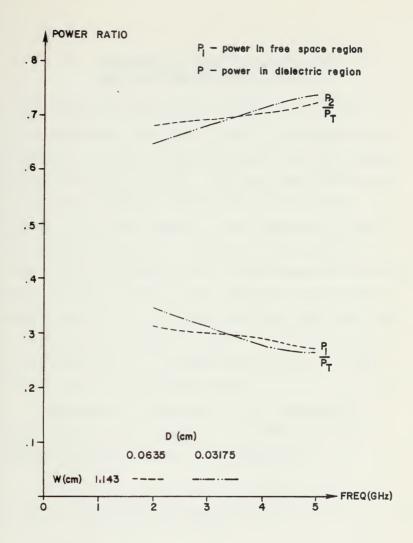


Figure 10. Average Power Ratio in Regions 1 and 2 Vs. Frequency for  $\epsilon_{\rm r}$  = 16.

# III. PERTURBATION ANALYSIS OF EDGE-GUIDED MODE ISOLATOR ON FERRITE SUBSTRATE

### A. PERTURBATION EXPRESSION FOR PROPAGATION CONSTANT

Perturbational analysis is used to determine solutions for perturbed problems slightly changed from other problems to which solutions are known. The study that was done up to this point obtained a solution for the propagation constant of an electro-magnetic wave traveling in a structure as shown in Figure 3. The goal of this study as was stated in the introduction, was to investigate the characteristics of waves traveling in the same structure as shown in Figure 3 but built on a ferrite substrate. This goal could be achieved by using the perturbation approach considering the dielectric case as the unperturbed problem, and the ferrite case as the perturbed problem.

A perturbational expression for the propagation constant due to small changes of a material type in a guidance structure is given in reference 8 as

$$\gamma' + \gamma^* = \frac{j\omega \int \left[ \left( \varepsilon_0 \left[ \Delta \chi_e \right] \cdot \vec{E}' \cdot \vec{E}^* \right) + \left( \mu_0 \left[ \Delta \chi_m \right] \cdot \vec{H}' \cdot \vec{H}^* \right) \right] ds}{\int \left[ \left( \vec{E}^* \chi \vec{H}' + \vec{E}' \chi \vec{H}^* \right) \cdot \vec{a}_z \right] ds}$$
(133)

where primes denote perturbed quantities.

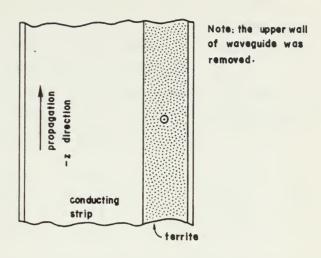
When external magnetic susceptibility is used, and assuming that the dielectric constant remains unchanged, hence  $[\Delta x_e^e] = 0$  then unperturbed magnetic and electric fields are used instead of the perturbed ones, and equation (133) can be rewritten as

$$\gamma' + \gamma * = \frac{j_{\omega\mu_0} \int_{\Delta S} \left[\chi_m^e\right] \cdot \bar{H} \cdot \bar{H}^* ds}{\int_{\int S} \left(\bar{E} * \chi \bar{H} + \bar{E} \chi \bar{H}^*\right) \cdot \bar{a}_{\chi} ds}$$
(134)

In the above equation the following notations are used

$\gamma' = \alpha'$	+ jβ'	perturbed propagation constant
$\gamma = \alpha + $	јβ	unperturbed propagation constant
ΔS		cross section of waveguide which is perturbed by a change of the material type
S		waveguide cross section
$\chi_{m}^{e}$		external magnetic susceptibility tensor
H and E		unperturbed magnetic and electric fields

The external D.C. magnetic field is applied perpendicular to the direction of propagation as shown in Figure 11.



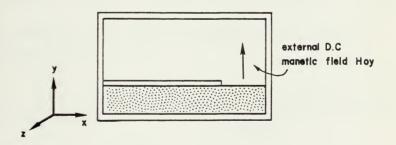


Figure 11. Shielded Isolator Structure.

According to reference 1 the lines of the magnetic field lie in Z-X plane hence an interaction between the R.F. field and the ferrite results when the D.C. magnetic field is applied perpendicular to Z-X plane.

The direction of the applied magnetic field implies no R.F. demagnetization in the y direction. Thus the external magnetic susceptibility tensor is given by

$$[x_{m}^{e}] = \begin{bmatrix} x_{xx} & 0 & x_{xz} \\ 0 & 0 & 0 \\ x_{zx} & 0 & x_{zz} \end{bmatrix} = \begin{bmatrix} x_{xx\bar{a}x\bar{a}x} + x_{xz\bar{a}x\bar{a}z} + x_{zz\bar{a}z\bar{a}z} \\ + x_{zx\bar{a}z\bar{a}x} + x_{zz\bar{a}z\bar{a}z} \end{bmatrix}$$
(135)

and the integrand in the numerator of equation (133) can be explicitly written as

$$[x_m^e] \cdot \bar{H} \cdot \bar{H}^* = [x_{xx}H_x + x_{xz}H_z]H_x^* + [x_{zx}H_x + x_{zz}H_z]H_z^*$$
 (136)

The denominator of equation is simply 4Pave so one can rewrite equation (134) as

$$\gamma' + \gamma^* = j\omega\mu_0 \frac{\int_0^D \int_0^C (\chi_{xx} |H_x|^2 + \chi_{zz} |H_z|^2 + \chi_{xz} H_z H_x^* + \chi_{zx} H_x H_z^*) dxdy}{4 \text{ Pave}}$$

# B. MAGNETIC SUSCEPTIBILITY TENSOR ELEMENTS

According to small signal approximation of the equation of motion in reference 8 two frequencies can be defined as

$$\omega_{z} = (\omega_{o} - N_{y} \omega_{m} + N_{z} \omega_{m}) = \omega_{o} - \omega_{m}$$
 (138)

$$\omega_{X} = (\omega_{0} - N_{V} \omega_{m} + N_{X} \omega_{m}) = \omega_{0} - \omega_{m}.$$
 (139)

where

 $\omega_0 = \gamma Hoy$ 

 $\omega_{\rm m} = \gamma 4\pi M_{\rm S}$ 

 $\gamma = 1.4 \cdot g[MHz/oe] = 0.879 \cdot g[Mrad/oe]$ 

g = Lande' factor (≈ 2)

Hoy = applied D.C. magnetic field in y direction [oe]

 $4\pi M_s$  = saturation magnetization [Gauss]

 $N_x, N_y, N_z$  = Demagnetization factors (in this case  $N_x = N_z = 0$ ,  $N_y = 1$ )

Define the ellipticity of the normal modes of the uniform precession [Ref. 8] as:

$$e_{o} = \sqrt{\frac{\omega_{X}}{\omega_{Z}}}$$
 (140)

and Kittel resonance relation for an ellipsoid [Refs. 8 and 9]

$$\omega_r = \sqrt{\omega_x \cdot \omega_z}$$

The Landau-Lifshitz damping factor is defined in reference 9 as

$$\alpha = \frac{\gamma \Delta H}{2\omega} \tag{141}$$

where AH is the line width of the ferrite.

In this study the ellipticity  ${\bf e}_0$  is equal to 1 and  $\omega_{\bf r}$  =  $\omega_0$  -  $\omega_{\bf m}$ , so by taking

$$\chi = \chi' - j\chi'' \tag{142}$$

and knowing that [Ref. 8]

$$\chi_{XZ} = -\chi_{ZX} \tag{143}$$

then the susceptibility elements can be expressed as

$$\chi'_{XX} = \chi'_{ZZ} = \frac{\omega_m \omega_r (\omega_r^2 - \omega^2) + \omega_m \omega_r \omega^2 \alpha^2}{\Delta}$$
(144)

$$\chi''_{XX} = \chi''_{ZZ} = \frac{\omega_{m}\omega_{\alpha}[\omega_{r}^{2} + \omega^{2}(1+\alpha^{2})]}{\Delta}$$
 (145)

$$\chi'_{XZ} = -\chi'_{ZX} = j \frac{\omega \cdot \omega_{m} \left[\omega_{r}^{2} - \omega^{2} (1+\alpha^{2})\right]}{\Delta}$$
 (146)

$$\chi''_{XZ} = -\chi''_{ZX} = j \frac{2\omega^2 \omega_m \omega_r \alpha}{\Delta}$$
 (147)

and

$$\Delta = \left[\omega_{r}^{2} - \omega^{2}(1 + \alpha^{2})\right]^{2} + 4\omega_{r}^{2}\omega^{2}\alpha^{2} \tag{148}$$

Since  $\chi_{XX} = \chi_{ZZ}$  and  $\chi_{XZ} = -\chi_{ZX}$  then one can simplify the perturbation expression given in equation (137) as follows

$$\gamma' + \gamma^* = j\omega\mu_0 = \frac{\int_0^D \int_0^D \left[\chi_{xx}(|Hx|^2 + |H_z|^2) + \chi_{xz}(H_zH_{yx}^* - H_z^*H_x)\right]}{4 \text{ Pave}}$$
 (149)

# C. COMPUTATION OF PERTURBATION EXPRESSION IN THE

In order to solve the perturbation expression [Eq. 149], the magnetic fields,  $\rm H_X$  and  $\rm H_Z$  were substituted in terms of the scalar potentials as follows

$$\gamma' + \gamma^* = \frac{j\omega\mu_0}{4Pave} \int_{00}^{DA} \left\{ x_{xx} \left[ \left( \frac{1}{2} j\beta \frac{\partial \phi_2^h(x,y)}{\partial x} + j\omega\epsilon_2 \frac{\partial \phi_2^e(x,y)}{\partial y} \right) \right] \right\} (150)$$

$$(\mp j\beta \frac{\partial \phi_2^h(x,y)}{\partial x} - j\omega\epsilon_2 \frac{\partial \phi_2^e(x,y)}{\partial y} + Kc_2^4 \phi_2^h(x,y) + Cc_2^4 \phi_2^h(x,y) + Cc_2^4 \phi_2^h(x,y) \right] + 2x_{xz} \left[ Kc_2^2 \phi_2^h(x,y) \left( \mp j\beta \frac{\partial \phi_2^h(x,y)}{\partial x} - j\omega\epsilon_2 \frac{\partial \phi_2^e(x,y)}{\partial y} \right) \right] \right\} dxdy.$$

The upper and lower signs denote waves traveling in negative and positive z-directions respectively.

Apply Parseval's theorem

$$\gamma' + \gamma * = \frac{j\omega\mu_0}{4PaveA} \sum_{n=-\infty}^{n=-\infty} \int_0^D \left\{ x_{xx} [(\beta^2\alpha_n^2 + Kc_2^4)] \phi_2^h(\alpha n, y)]^2 + (15) \right\}$$

$$\mp j\beta\alpha n\omega\epsilon_2 (\phi_2^h(\alpha n, y)) \frac{\partial \phi_2^h(\alpha n, y)}{\partial y} - \phi_2^h(\alpha n, y) \frac{\partial \phi_2^h(\alpha n, y)}{\partial y}) + (15)$$

$$+ \omega^{2} \varepsilon_{2}^{2} \left| \frac{\partial \Phi_{2}^{e}(\alpha n, y)}{\partial y} \right|^{2} +$$
 (151)

$$+ \ 2\chi_{\chi\chi} \text{Kc}_2^2 \phi_2^h(\alpha n,y) \big[ \underline{+} \beta \alpha n \phi_2^{h^{\displaystyle *}}(\alpha n,y) \ - \ j_{\omega\epsilon} 2^{\displaystyle \frac{\partial \phi_2^{e^{\displaystyle *}}}{\partial y}} \big] \bigg\} \ dy.$$

The integration with respect to y was computed analytically for both regions where  $\gamma_2$  is either a real or an imaginary quantity.

Recall equations (49) through (52)

$$\Phi_{2}^{h}(\alpha n, y) = \begin{cases} C_{H}^{h}(\alpha n) \cosh \gamma_{2}y & \gamma_{2} \text{ real} \\ C_{T}^{h}(\alpha n) \cos \gamma_{2}"y & \gamma_{2} \text{ imaginary} \end{cases}$$

$$\frac{\partial \Phi_2^e(\alpha n, y)}{\partial y} = \begin{cases} \gamma_2 D_H^e(\alpha n) \cosh \gamma_2 y & \gamma_2 \text{ real} \\ \gamma_2 D_T^e(\alpha n) \cos \gamma_2 y & \gamma_2 \text{ imaginary.} \end{cases}$$

Substituting into equation (151) for both hyperbolic and trigonometric cases, and integrating with respect to y, one can obtain:

For the hyperbolic case (152) 
$$\gamma' + \gamma * = \frac{j\omega\mu_0}{8PaveA} \sum_{n=-\infty}^{n=-\infty} \left\{ x_{XX} \left[ \frac{\sinh 2\gamma_2 D}{2\gamma_2} + D \right] \left[ \left( \beta^2 \alpha n^2 + Kc_2^2 \right) \left| C_H^h(\alpha n) \right|^2 + \omega^2 \varepsilon_2^2 \gamma_2^2 \left| D_H^e(\alpha n) \right|^2 + j\beta\alpha n\omega\gamma_2 \varepsilon_2 \left( C_H^h(\alpha n) D_H^{e*}(\alpha n) - C_H^{h*}(\alpha n) D_H^e(\alpha n) \right] - c_H^{h*}(\alpha n) D_H^e(\alpha n) \right] - j2\chi_{XZ} Kc_2^2 \omega \varepsilon_2 \gamma_2 D_H^{e*}(\alpha n) C_H^h(\alpha n) \left[ \frac{\sinh 2\gamma_2 D}{2\gamma_2} + D \right]$$

And similarly for the trigonometric case

$$\begin{split} \gamma' + \gamma^* &= \frac{j_{\omega_D}}{8PaveA} \sum_{n=-\infty}^{\infty} \left\{ x_{XX} \left[ \frac{\sin 2\gamma_2^{"D}}{2\gamma_2^{"}} + D \right] \left[ (\beta^2 \alpha n^2 + Kc_2^2) \cdot | c_T^h(\alpha n)|^2 \right] \right. \\ &+ \left. \omega^2 \varepsilon_2^2 \gamma_2^{"2} | D_T^e(\alpha n)|^2 + \beta \alpha n \omega \varepsilon_2 \gamma_2^{"} \left( C_T^h(\alpha n) D_T^{e*}(\alpha n) + C_T^{h*}(\alpha n) D_T^e(\alpha n) \right) \right] - \\ &+ \left. c_T^{h*}(\alpha n) D_T^e(\alpha n) \right] - \\ &- 2 \chi_{XZ} K c_2^2 \omega \varepsilon_2 \gamma_2^{"D} D_T^{e*}(\alpha n) C_T^h(\alpha n) \left[ \frac{\sin 2\gamma_2^{"D}}{2\gamma_2^{"}} + D \right] \right\} . \end{split}$$

D. COMPUTATION OF NORMALIZED PHASE CONSTANT AND ATTENUATION The perturbed and unperturbed propagation constants have the form of

$$\gamma' = \alpha' + j\beta'$$
 (154)  
 $\gamma = j\beta \ (\alpha = 0 \text{ for dielectric case})$ 

Thus the left hand side of the perturbation expression is equal to

$$\gamma' + \gamma^* = \alpha' + j\beta' + (-j\beta) = \alpha' + j(\beta' - \beta) \tag{155}$$

Using equation (155) one can obtain

$$\alpha' + j(\beta' - \beta) = \frac{j\omega\mu_0}{8Pave \cdot A} \sum_{n=-\infty}^{\infty} (R_E + jI_m)$$
 (156)

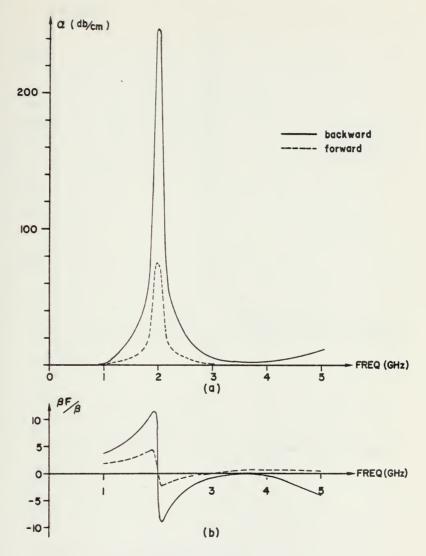


Figure 12. a) Attenuation and b) Normalized Propagation Constant for Waves Traveling in +Z and -Z Directions for:  $\Delta H = 75~\text{Op},~H_{D.C} = 1916.3~\text{op},\\ 4\pi\text{MS} = 1200~\text{Ga},~g = 1.99~\text{c}_r = 15.2$ 

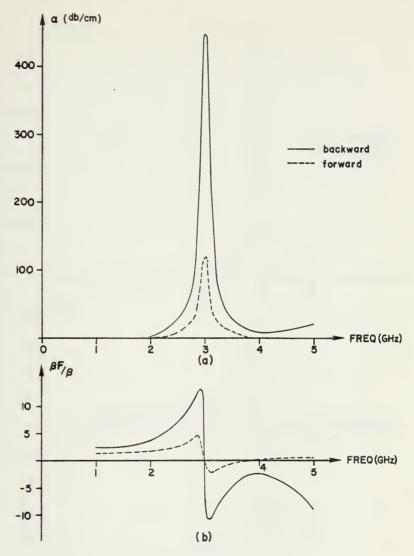


Figure 13. a) Attenuation and b) Normalized Propagation Constant for Waves Traveling in +Z and -Z Directions for:  $\Delta H = 750e, \ H_{D} \ c = 2271.420e, \\ 4\pi MS = 1200 \ Gac g = 1.99, \ \epsilon_r = 15.2$ 

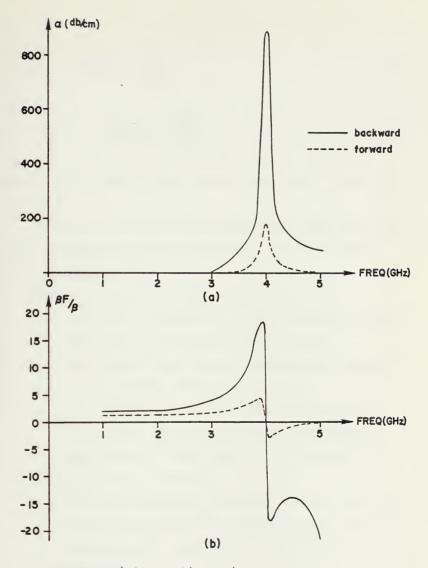


Figure 14. a) Attenuation and b) Normalized Propagation Constant for Waves Traveling in +Z and -Z Directions for:  $\Delta H = 75 \text{ oe, } H_{D.C} = 2628.6 \text{ oe,} \\ 4\pi MS = 1200 \text{ Ga, } g = 1.99, \epsilon_r = 15.2$ 

or

$$\alpha' = -\frac{\omega \mu_0}{8 \text{Pave} \cdot A} \sum_{m=-\infty}^{\infty} I_m$$
 (157)

$$\beta'/\beta = 1 + \frac{\omega \mu_0}{8 \text{PaveA} \cdot \beta} \sum_{n=-\infty}^{\infty} R_E$$
 (158)

Detailed development of the last two equations is given in appendix B.

Figures 12, 13 and 14 were plotted for three different values of external magnetic fields Hoy, hence for three different resonant frequencies.

Several facts can be studied from these plots.

- a. The ratio of backward to forward attennuation is very large, as required for an isolator.
- b. Both backward and forward attenuations increase as the resonant frequency increases.
- c. The ratio of backward to forward attenuation increases as the resonant frequency increases.
- d. The bandwidth of the isolator is determined by the ferrite linewidth.
- e. The normalized phase constants in both directions are frequency dependent and exceed high values as approaching the lower side of the isolator's bandwidth.

The region of negative values of normalized phase constants was not investigated, thus at present no explanation is obtained. Hopefully laboratory measurements will indicate whether it was an error due to the inherent approximations of the perturbational technique, or how large are the deviations from the correct results.

# IV. COMPUTER PROGRAMMING

The computer program that was developed for this study was written in FORTRAN IV language and has three major steps:

- 1. Computing wavelength ratio  $\lambda'/\lambda$ , for waves traveling in a device built on dielectric substrate (Fig. 3).
- Computing power flow in a device built on dielectric substrate.
- 3. Computing normalized phase constant  $\beta F/\beta$ , and attenuation in db/cm for waves traveling in a device built on ferrite substrate (Fig. 3). These computations were done for both forward and backward directions of propagation.

The computations of the wavelength ratio in step 1 were made by finding the root  $\beta$  that solved the determinental equation (113). First, equation (113) was solved for an arbitrary value of  $\beta$ , and then, by the use of Newton-Raphson iteration method,  $\beta$  was computed until the change between two  $\beta$ 's in two successive iterations was in the 6th or 7th digit after the decimal point. From the value of the last  $\beta$ ,  $\lambda$ '/ $\lambda$  could easily be computed.

In step 2 the power flow was computed for both hyperbolic and trigonometric cases, depending whether  $\gamma_2$  was a real or imaginary quantity. The computed  $\beta$ , and the coefficient ratio  $a_2/a_1$  obtained in part 1, were used as entries in part 2.

In step 3 both power flow and computed  $\beta$  were used as entries. This step was executed twice each time for waves traveling in both directions. The output of this step could be obtained for only one value of the following parameter at each run:

Ferrite linewidth
Applied D.C. magnetic field
Saturation magnetization and
Lande'-g of the ferrite.

All three steps could be calculated for different values of frequencies strip's width and substrate's thickness in one run.

The required input data to the program is given in Appendix C.

The limits for all summations in the program were chosen by a trial and error method, since there were no definite limits that could be pointed out.

The upper and lower frequencies of operation are bounded as follows.

Lower frequency is bounded by the strip's width such as

$$\frac{\lambda_0 \max}{4\sqrt{\epsilon r_2}} = W \tag{159}$$

or

$$f_{\min} = \frac{c}{4W \varepsilon r_2}$$
 (160)

Approximated upper bound was applied according to reference 10. This reference discusses the case of a rectangular guide with dielectric slab perpendicular to the electric field as shown in Figure 15.

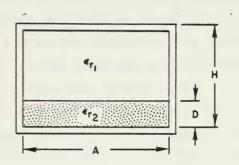


Figure 15. Waveguide Filled with Dielectric Slab Perpendicular to the Electric Field.

The guided wavelength is given as

$$\lambda_{g} = \frac{\lambda_{o}}{\sqrt{\frac{\varepsilon r_{1}}{1 - \frac{D}{H}(1 - \frac{\varepsilon r_{1}}{\varepsilon r_{2}})} - (\frac{\lambda_{o}}{2})^{2}}}$$
(161)

The cut-off wavelength of this guide is the one that set the denominator equal to zero, so from equation (161) one can obtain

$$\lambda_{\text{o min}} = 2 A \sqrt{\frac{\epsilon_{\text{r1}}}{1 - \frac{D}{H}(1 - \frac{\epsilon_{\text{r1}}}{\epsilon_{\text{r2}}})}}$$
 (162)

and 
$$f_{\text{max}} = \frac{C}{\lambda_{\text{omin}}}$$
 (163)

# V. CONCLUSIONS

In this study a theoretical analysis of a model for a shielded edge-guided mode isolator was presented.

The analysis was based on a complete solution for an unperturbed problem (the dielectric case) and then by the use of a perturbation technique, a solution was derived for a perturbed problem, (the ferrite case).

Final results indicated that above and below the resonant frequency the forward attenuation is very low - negligible, while the reverse attenuation is high. These are good regions in which to operate as an isolator. One result which is still unexplained is that the normalized phase constant is negative in the frequency region above the resonant frequency.

A computer program was developed for all steps of the theoretical analysis.

#### APPENDIX A

# AVERAGE POWER FLOW IN REGIONS 1 and 2

Equation (129) indicates the total power flow in region 1. In order to solve this equation both  $\bar{A}^e$  and  $\bar{A}^h$  should be known explicitly.

Recall

$$\bar{A}^{e}(n) = \frac{E_{z}(\alpha n)}{Kc_{1}^{2}\sinh\gamma_{1}(D-H)}$$
(A-1)

$$\bar{A}^{h}(\alpha n) = -j\left[\frac{\alpha n \beta E_{z}(\alpha n)}{K c_{1}^{2}} - E_{x}(\alpha n)\right] \frac{1}{\omega \mu_{1} \gamma_{1} \sin h \gamma_{1}(D-H)}$$
 (A-2)

$$E_{\chi}(\alpha n) = M_1^{H,T}(\alpha n,\beta)J_{\chi}(\alpha n) + M_2^{H,T}(\alpha n,\beta)J_{\chi}(\alpha n)$$
 (A-3)

$$E_{z}(\alpha n) = M_{3}^{H,T}(\alpha n,\beta)J_{x}(\alpha n) + M_{4}^{H,T}(\alpha n,\beta)J_{z}(\alpha n) \qquad (A-4)$$

Since  $M_1^{H,T}(\alpha n,\beta)$ ,  $M_2^{H,T}(\alpha n,\beta)$ ,  $M_3^{H,T}(\alpha n,\beta)$  and  $M_4^{H,T}(\alpha n,\beta)$  are imaginary quantities, one can define

$$M_1^{H,T}(\alpha n,\beta) = jm_1^{H,T}(\alpha n,\beta)$$

$$M_{2}^{H,T}(\alpha n,\beta) = jm_{2}^{H,T}(\alpha n,\beta)$$

$$M_{3}^{H,T}(\alpha n,\beta) = jm_{3}^{H,T}(\alpha n,\beta)$$
(A-5)

$$M_A^{H,T}(\alpha n,\beta) = jm_A^{H,T}(\alpha n,\beta)$$

Furthermore, referring to equation (115) one can assume that  $\mathbf{a}_2$  is a real quantity and  $\mathbf{a}_1$  is imaginary quantity. So one can write

$$a_1 = j\bar{a}_1 \tag{A-6}$$

where  $\bar{a}_1$  is real quantity.

Substituting equation (A-5), (A-6), (110) and (111) into equations (A-3) and (A-4) one can obtain

$$E_{\chi}(\alpha n) = E_{\chi_{1}}(\alpha n) + jE_{\chi_{2}}(\alpha n)$$
 (A-7)

$$E_{z}(\alpha n) = E_{z_{1}}(\alpha n) + jE_{z_{2}}(\alpha n)$$
 (A-8)

where

$$E_{x_1}(\alpha n) = \bar{a}_1 \left[ -\frac{a_2}{\bar{a}_1} m_1^{H,T}(\alpha n,\beta) g_{x_0}(\alpha n) - (A-9) \right]$$

- 
$$m_2^{H,T}(\alpha n,\beta)f_{ze}(\alpha n)$$

$$\mathbb{E}_{x_2}(\alpha n) = \bar{a}_1 \left[ \frac{a_2}{\bar{a}_1} \cdot m_1^{H,T}(\alpha n,\beta) g_{xe}(\alpha n) - (A-10) \right]$$

- 
$$m_2^{H,T}(\alpha n,\beta)$$
  $f_{zo}(\alpha n)$ 

$$E_{z_{1}}(\alpha n) = \bar{a}_{1}[-\frac{a_{2}}{\bar{a}_{1}} m_{3}^{H,T}(\alpha n,\beta) g_{x_{0}}(\alpha n) - - m_{A}^{H,T}(\alpha n,\beta) f_{z_{0}}(\alpha n)]$$
(A-11)

$$E_{z_{2}}(\alpha n) = \bar{a}_{1} \left[ \frac{a_{2}}{\bar{a}_{1}} m_{3}^{H,T}(\alpha n,\beta) g_{xe}(\alpha n) - - m_{4}^{H,T}(\alpha n,\beta) f_{zo}(\alpha n) \right]$$
(A-12)

and

$$\frac{a_2}{\bar{a}_1} = \frac{\sum_{n=-\infty}^{\infty} m_2^{H,T}(\alpha n,\beta)B(\alpha n)}{\sum_{n=-\infty}^{\infty} m_1^{H,T}(\alpha n,\beta)|g_{\bar{X}}(\alpha n)|^2}$$
(A-13)

After investigating equations (A-9) through (A-12) it could be seen that  $E_{\chi_1}(\alpha n)$  and  $E_{Z_2}(\alpha n)$  are even functions, while  $E_{\chi_2}(\alpha n)$  and  $E_{Z_1}(\alpha n)$  were odd functions. Substitution of these functions into equations (A-1) and (A-2) led to explicit expresions of  $\bar{A}^e(\alpha n)$  and  $\bar{A}^h(\alpha n)$ , hence the power flow in region 1 could be calculated.

It is clear that the power flow in region 2 for both the hyperbolic and trigonometric cases could be calculated in the same way since the coefficients  $D_H^e(\alpha n)$ ,  $C_H^h(\alpha n)$ ,  $D_T^e(\alpha n)$  and  $C_T^h(\alpha n)$  are functions of  $E_X^e(\alpha n)$  and  $E_Z^e(\alpha n)$  which their explicit expressions are given in equations (A-9) through (A-12).

#### APPENDIX B

## NORMALIZED PHASE CONSTANT AND ATTENUATION

As was stated in equation (157) and (158)

$$\alpha' = -\frac{\omega \mu_0}{8 Pave A} \sum_{n=-\infty}^{\infty} I_m$$
 (B-1)

$$\beta'/\beta = 1 + \frac{\omega \mu_0}{8 PaveA} \sum_{n=-\infty}^{\infty} R_E$$
 (B-2)

So in order to calculate  $\alpha'$  and  $\beta'/\beta$  , both  $\boldsymbol{I}_m$  and  $\boldsymbol{R}_E$  should be known explictly.

For the <u>hyperbolic case</u>, equation (151) had to be divided into real and imaginary components.

Recall equations (67) and (68) and substrate equations (A-7) and (A-8) for  $E_{\rm X}(\alpha n)$  and  $E_{\rm Z}(\alpha n)$  one can obtain

$$C_{H}^{h}(\alpha n) = \frac{1}{\omega \mu_{2} \gamma_{2} \sin h \gamma_{2} D} \left\{ \left[ -\frac{\beta \alpha_{n}}{K c_{2}^{2}} E_{z_{2}}(\alpha n) + E_{x_{2}}(\alpha n) \right] + (B-3) \right\}$$

+ 
$$j\left[\frac{\beta\alpha_n}{Kc_2}\right]^2 E_{Z_1}(\alpha n) - E_{X_1}(\alpha n)$$

$$D_{H}^{e}(\alpha n) = \frac{1}{Kc_{2}^{2} \sinh_{\gamma_{2}} D} \left[ \mathbb{E}_{z_{1}}(\alpha n) + j \mathbb{E}_{z_{2}}(\alpha n) \right]$$
 (B-4)

Substituting equations (B-3) and (B-4) into equation (152) and separating to real and imaginary parts, the following equations are obtained

$$RI_{1} = \frac{\beta^{2} \alpha n^{2} + Kc_{2}^{2}}{\omega^{2} \mu_{2}^{2} \gamma_{2}^{2}} \left\{ \left[ -\frac{\beta \alpha n}{K_{2}^{2}} E_{z_{2}}(\alpha n) + E_{x_{2}}(\alpha n) \right]^{2} + (B-5)^{2} + \left[ \frac{\beta \alpha n}{Kc_{2}^{2}} E_{z_{1}}(\alpha n) - E_{x_{1}}(\alpha n) \right]^{2} \right\} + \left[ \frac{\beta^{2} \alpha n}{Kc_{2}^{2}} E_{z_{1}}(\alpha n) - E_{x_{1}}(\alpha n) \right]^{2} + \left[ \frac{\omega^{2} \varepsilon_{2}^{2} \gamma_{2}^{2}}{Kc_{2}^{4}} \left[ E_{z_{1}}^{2}(\alpha n) + E_{z_{2}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] - \left[ \frac{2\beta \alpha n}{Kc_{2}^{2}} \left[ \frac{\beta \alpha n}{K_{2}^{2}} \left[ E_{z_{1}}^{2}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] - E_{z_{2}^{2}}(\alpha n) \right] \right\}$$

$$RI_{2} = \frac{\varepsilon_{2}}{\mu_{2}^{2}} \left[ E_{x_{1}}(\alpha n) E_{z_{2}^{2}}(\alpha n) - E_{x_{2}^{2}}(\alpha n) - E_{x_{2}^{2}}(\alpha n) \right]$$

$$(B-6)$$

$$Im = \left[\frac{ctgh\gamma_{2}D}{\gamma_{2}} + \frac{D}{sinh^{2}\gamma_{2}D}\right]\left[-\frac{x_{xx}^{"}}{2}RI_{1} - \frac{x_{xz}^{"}}{2}RI_{2}\right] \quad (B-8)$$

(B-7)

 $RE = \left[\frac{\operatorname{ctgh}_{\gamma_2}^{\mathsf{D}}}{\gamma_2} + \frac{\mathsf{D}}{\operatorname{sinh}_{\gamma_2}^{\mathsf{D}}}\right] \left[\frac{\mathsf{X}_{\mathsf{X}\mathsf{X}}^{\mathsf{L}}}{2} \operatorname{RI}_1 + \frac{\mathsf{X}_{\mathsf{X}\mathsf{Z}}^{\mathsf{L}}}{2} \operatorname{RI}_2\right]$ 

Similarity for the <u>trigonometric case</u> the coefficients  $C_T^h(\alpha n)$  and  $D_T^e(\alpha n)$  can be expressed in terms of  $E_\chi(\alpha n)$  and  $E_{\chi}(\alpha n)$  as follows

$$C_{T}^{h}(\alpha n) = \frac{1}{\omega \mu_{2} \gamma_{2}^{"} \sin \gamma_{2}^{"} D} \left\{ \begin{bmatrix} \frac{\beta \alpha n}{K c_{2}^{2}} & E_{z_{2}}(\alpha n) - E_{x_{2}}(\alpha n) \end{bmatrix} + (B-9) \right\}$$

$$+ j \left[ -\frac{\beta \alpha n}{K c_{2}^{2}} & E_{z_{1}}(\alpha n) + E_{x_{1}}(\alpha n) \right]$$

$$D_{T}^{e}(\alpha n) = -j \frac{1}{Kc_{2}^{2} sin\gamma_{2}^{n}} E_{z}(\alpha n)$$
(B-10)

and both the real and imaginary parts of equation (152) have the form of

$$RI_{1} = \frac{\beta^{2} \alpha n^{2} + KC_{2}^{2}}{\omega^{2} \mu_{2}^{2} \gamma_{2}^{n^{2}}} \left\{ \left[ \frac{\beta \alpha n}{Kc_{2}^{2}} E_{z_{2}}(\alpha n) - E_{x_{2}}(\alpha n) \right]^{2} + (B-11) \right\}$$

$$+ \left[ -\frac{\beta \alpha n}{Kc_{2}^{2}} E_{z_{1}}(\alpha n) + E_{x_{1}}(\alpha n) \right]^{2} + \left[ +\frac{\omega^{2} \varepsilon_{2}^{2} \gamma_{2}^{n^{2}}}{Kc_{2}^{4}} \left[ E_{z_{1}}^{2}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right]^{2} + \left[ +\frac{2\beta \alpha n}{Kc_{2}^{2}} \left[ E_{z_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2\beta \alpha n}{Kc_{2}^{2}} \left[ \frac{\beta \alpha n}{Kc_{2}^{2}} \left[ E_{z_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] - \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) - E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) + E_{z_{2}^{2}}(\alpha n) \right] \right] + \left[ -\frac{2}{2} \left[ \frac{(\alpha n)}{2} E_{x_{1}^{2}}(\alpha n) +$$

$$RI_{2} = -\frac{\varepsilon_{2}}{\mu_{2}} \left[ E_{X_{1}}(\alpha n) E_{Z_{2}}(\alpha n) - E_{X_{2}}(\alpha n) E_{Z_{1}}(\alpha n) \right]$$
 (B-12)

$$R_{E} = \left[\frac{D}{\sin^{2}\gamma_{2}^{"}D} + \frac{\cot g\gamma_{2}^{"}D}{\gamma_{2}^{"}}\right] \left[\frac{x_{xx}^{'}}{2} RI_{1} + \frac{x_{xz}^{'}}{2} RI_{2}\right]$$
 (B-13)

$$I_{m} = \left[\frac{D}{\sin^{2}\gamma_{2}^{"}D} + \frac{\cot g\gamma_{2}^{"}D}{\gamma_{2}^{"}}\right] \left[-\frac{\chi_{xx}^{"}}{2} RI_{1} - \frac{\chi_{xz}^{"}}{2} RI_{2}\right]$$
 (B-14)

After substituting properly equations (B-7), (B-8), (B-13) and (B-14) into equations (B-1) and (B-2) the later can be solved for the attenuation and normalized phase constant.

### APPENDIX C

# COMPUTER PROGRAM

THEORY OF FIELD DISPLACEMENT DEVICES

SHEILDED EDGE GUIDED MODE ISOLATOR (BOX'S DIMENSION 0.4''\*0.9'')

THIS PROGRAM HAS THREE MAJOR STEPS CORRESPONDING TO THE STEPS OF THE THEORETICAL ANALYSIS OF THE DEVICE THE THREE STEPS ARE:

1.COMPUTING WAVELENGTH RATIO OF THE DEVICE BUILT ON DIELECTRIC SUBSTRATE.

2.COMPUTING POWER FLOW IN THE DEVICE.

3.COMPUTING NORMALIZED PROPAGATION CONSTANT AND ATTENUATION IN CB PER CM OF FERRITE BUILT DEVICE BY USING PERTUREATION THEORY AND DATA CETAINED IN STEPS 1 & 2. THE DEVICE.

PROGRAM ACCEPTS FOLLOWING DATA:

1.FIRST CARD-L1,M1,MN1 FORMAT(3(12,X2))
L1 -NUMBER OF FREQ. CATA CARDS.
M1 -NUMBER OF STRIP WIDTHS DATA CARDS.
MN1-NUMBER OF SUBSTRATE THICKNESS DATA CARDS.

2.SECOND CARD-(FREQ(L),L=1,L1) FORMAT(D9.3) FREQ(L) ARE THE FREQUENCIES IN HERTZ AT WHICH THE COMPUTATIONS ARE EXECUTED. NUMBER OF "SECOND" CARDS=L1.

3.THIRD CARD-(W(M), M=1, M1) FORMAT(D10.4) W(M) ARE THE VARIGUS STRIP WIDTHS, IN METERS. NUMBER OF ''THIRD'' CARDS=M1.

4.FOURTH CARD-(D(MN), MN=1, MN1) FORMAT(D10.4)
D(MN) ARE THE VAPIOUS SUBSTRATE THICKNESS, IN METERS.
NUMBER OF ''FOURTH'' CARDS=MN1.

5.FIFTH CARD-EPSR FORMAT(F5.2). EPSR- RELATIVE DIELECTRIC CONSTANT.

6.SIXTH CARD-DELTH FGRMAT(D12.3)
DELTH-LINEWIDTH OF FERRITE IN CERSTEDS.

7.SEVENTH CARD-HO FORMAT(D12.3)
HO-APPLIED D.C MAGNETIC FIELD IN DERSTEDS.

8.EIGHTH CARD-AMAGS FORMAT(D12.3)
AMAGS-SATURATION MAGNETIZATION IN GAUSS.

9.NINTH CARD-G FORMAT(F4.2) G- LANDE-G OF FERRITE.

## CUTPUT:

1. WAVELENGTH RATIO FOR DIELECTRIC SUBSTRATE.

2.NCRMALIZED PROPAGATION CONSTANT FOR BACKWARD AND FORWARD DIRECTIONS OF PROPAGATION.

3.ATTENUATION FOR BACKWARD AND FORWARD DIRECTIONS OF PROPAGATION.

THE OUTPUT IS PRINTED FOR ALL FREGUENCIES, STRIP WIDTHS AND SUBSTRATE THICKNESS.

THE UPPER AND LOWER FREQUENCIES OF OPERATION ARE BOUNDED TO ELIMINATE UNDESIRED MODES OF : MCITUAD

```
PROPAGATION IN THE DEVICE.
ALL COMPUTATIONS ARE PERFORMED IN OCUBLE PRECISION.
                LANGUAGE-FORTRAN
                PROGRAM DEVELOPED BY LT.J.G RAM SHARON THESIS ADVISOR- PROF. CR. J.B.KNORR. NAVAL POSTGRADUATE SCHOOL MONTEREY CAL
                                                                                                                             ISRAELI NAVY.
                                                                                                               CALTEGRATA
                FEBRUARY
                IMPLICIT REAL*8 (A-H,C-Z)
DIMENSION TOT(4), FREQ(10), W(8),D(8)
C
                ZZ=20.00
S=0.00
C
                FORMAT
FORMAT
FORMAT
FORMAT
FORMAT
                                   (D9.3)
(D10.4)
(3(I2,2X))
(F5.2)
(D12.3)
(F4.2)
        1
2
3
5
10
7
C
                (5,1)
(5,1)
(5,2)
(5,2)
(5,10)
(5,10)
(5,10)
(5,7)
                                              L1,M1,MN1
(FREQ(L),L=1,L1)
(W(M),M=1,M1)
(D(MN),MN=1,MN1)
EPSR
DELTH
HO
AMAGS
                                              G
C
                PI=5.141592654D0

AMU1=4.D0*PI*1.JD-7

AMUR=1.D0

AMU2=AMU1*AMUR

EPS1=1.D0/(36.D0*PI*1.D+9)

EPS2=EPS1*EPSR
00000
      STEP1-WAVELENGTH RATIO CALCULATIONS.
     H-BCX'S HEIGHT
                 H=1.016D-2
000
     A-BOX'S WIDTH
                 A=2.286D-2
      FPEQUENCY LOOP
                CO 4000 L=1,L1
FREQ1=FREQ(L)/1.00+9
OMEGA=2.00*PI*FREQ(L)
OMEGA1=GMEGA/1.00+9
WRITE (6,4)
FORMAT (///////)
      PRINT OUT OF
                                         INPUT DATA
                WRITE (6,199)
FORMAT (30X,22H********************************
WRITE (6,200) FREQ1
FORMAT (30X,8H* FREQ1=,F5.3,7H GHZ,2H *
WRITE (6,201) OMEGA1
FORMAT (30X,9H* OMEGA1=,F6.3,5H GRPS,2H *)
WRITE (6,202) H
FORMAT (30X,4H* H=,E11.4,5H MTR,2H *)
WRITE (6,203) A
WRITE (6,203) A
WRITE (6,203) A
WRITE (6,203) A
GORMAT (30X,4H* A=,E11.4,5H MTR,2H *)
WRITE (6,207) EPSR
FORMAT (30X,7H* EPSR=,F4.1,9X,2H *)
      159
                                                                                                             GHZ, 2H =)
      200
      201
      202
      203
```

```
206
    210
    212
    213
    208
           HIGHER FREQUENCY OF OPERATION
    SET
           GM=2.D0*A/DSQRT(1.D0-D(MN)/H*(1.DC-1.DC/EPSR))
FREQU=3.D8/GM
IF (FREQ(L).GE.FREQU) GC TO 40GC
000
   STRIP WIDTH LOOP
            DO 5000 M=1,M1
SET
           LOWER FREQUENCY OF OPERATION
   FREQL=(3.0C+08/DSQRT(EPSR))/(4*W(M))
IF (FREQ(L).LE.FREQL) GC TO 5000
WRITE (6,205) W(M)
205 FORMAT (10X,2HW=,F11.5//)
    SUBSTRATE THICKNESS LOOP
           D9 6000 MN=1,MN1
WRITE (6,209)
FORMAT (20X,14HLAMBDA'/LAMBDA,7X,1HD,15X,4HBETA/)
C
            N1=101
11=201
    BETA-PROPAGATION CONSTANT .
            DBETA=1.0D-1
BETA1=300.D0
  1000
           TOT(1)=20.00
DO 2000 K=1,2
            BETA=BETA1

IF (K•EC•2) GO TO 600

GO TO 700

BETA=BETA+DBETA

AK1=OMEGA*DSGRT(AMU1*EPS1)

AK2=OMEGA*DSGRT(AMU2*EPS2)

AK2=S=AK1**2-BETA**2

AKC2S=AK2**2-BETA**2
    600
C
            SUM1=0.000
SUM2=0.000
SUM3=0.000
TTPWR1=0.00
TTPWR2=0.00
TCTPWR=0.00
C
           N1=51

11=101

RE11=0.00

RE22=0.00

ZM11=0.00

ZM21=0.00

N=-N1
       16
        9
C
            DO 130 I=1,I1
            N=M+1
           ALFAN=2.DO*PI*N/A
GAMA1=DSQRT(ALFAN**2-AKC1S)
```

```
GAMA2S=ALFAN**2-AKC2S
GAMA2=DSQRT(DABS(GAMA2S))
A1=1.DQ/DTANH(GAMA1*(H-C{MN}))
A2=0MEGA*AMU1*GAMA1
A3=0MEGA*AMU2*GAMA2
A4=ALFAN*BETA
A5=0MEGA*EPS1*GAMA1/AKC1S
A6=0MEGA*EPS2*GAMA2/AKC2S
IF (GAMA2S.GE.O.DOC) GO TO 20
TRIGONOMETRIC CASE
                  A7=DTAN(GAMA2*D(MA))
F1=-AKC13*41/A2+AKC2S/(A7*A3)
F2=A4*A1/A2-A4/(A7*A3)
                   F3=-F2
                  F54-A4*x2*A1/(A2*AKC1S)-A5*A1-A4**2/(AKC2S*A7*A3)-A6/A7
HYPERBOLIC CASE
                  A8=1.D0/DTANH(GAMA2*D(MN))
F1=-AKC1S*A1/A2-AKC2S*A8/A3
F2=A4*A1/A2+A4*A8/A3
      20
                F1=-AKC13+A1/A2-AKC23+A0/A3
F2=-F2
F4=A4*A1/A2+A4*A8/A3
F3=-F2
F4=A4**2*A1/(A2*AKC1S)-A5*A1+A4**2*A8/(AKC2S*A3)-A6*A8
AM1=F4/DN
AM2=-F2/DN
AM3=-AM2
AM4=F1/DN
SN=DS1N(ALFAN*W(M))
CN=DCJS(ALFAN*W(M))
R1=DEXP(ZZ)
R2=(ZZ/W(M))**2+ALFAN**2
R3=R1*CN
R7=R1*SN
Q=((PI/(2*D0*W(M)))**2*ALFAN**2)
GX1=F1/(2*D0*W(M))**CN/C
GX2=(PI/(2*D0*W(M))*SN+ALFAN)/C
FZ1=(ZZ/W(M)*(R3-1*D0)*Z/W(M)*R7)/R2
FZ2=(-ALFAN*(R3-1*D0)*Z/W(M)*R7)/R2
FZ2=(-ALFAN*(R3-1*D0)*Z/W(M)*R7)/R2
FZ2=(-ALFAN*(R3-1*D0)*Z/W(M)*R7)/R2
FZ2=(-ALFAN*(R3-1*D0)*Z/W(M)*R7)/R2
FZ2=(-ALFAN*(R3-1*D0)*Z/W(M)*R7)/R2
FZ2=(-ALFAN*(R3-1*D0)*Z/W(M)*R7)/R2
FZ2=(-ALFAN*(R3-1*D+O1)*G0*T0*8
     30
STEP 2 -POWER FLOW CALCULATIONS.
                 AMP1=1.D-10
Z1=-SUM2/SUM3
Z3=Z1*GX1
Z2=Z1*GX2
Z1=AMP1*(-AM3*Z2-AM4*FZ1)
EZ2=AMP1*(-Z2*AM1-AM2*FZ1)
EX1=AMP1*(-Z2*AM1-AM2*FZ1)
EX1=AMP1*(-Z2*AM1-AM2*FZ1)
EX2=AMP1*(Z3*AM1-AM2*FZ1)
EX5=5Z1**2+EZ2**2
EX5=5Z1**2+EZ2**2
IF ($.$EQ.1.D0) GO TO 18
REGION 1 FREE SPACE
                  V0=GAMA1*(H-C(MN))
V1=DMEGA*BETA*EPS1/2.00
V2=1.00/(DTANH(V0)*GAMA1)
IF (V0.GE.85.00) GS TO 12
V3=(H-D(MN))/((DSINH(V0))**2)
                 V3=(H-D(MN))/((DSINH(V3))**2)
GC TO 11
V3=0001
V5=BETA/(2.DG*OMEGA*AMU1)
V4=ALFAN*8ETA/AKC1S
V6=(V4*EZ2-EX2)**2+(-V4*EZ1+EX1)**2
V7=V4*EZS-EZ1*EX1-EZ2*EX2
TR11=-V1*ALFAN**2/(AKC1S**2)*EZS*(V2-V3)
TR12=-V5*ALFAN**2/(GAMA1**2)*V6*(V2+V3)
TR13=-V5*V6*(V2-V3)
```

```
TR14=-V1*(GAMA1**2)/(AKC1S**2)*FIS*(V2+V3)
TR156=ALFAN/(DMEGA*AMU1*AKC1S)*(BETA**2+AK1**2)*V7*V2
PWR1=-(TR11+TR13+TR13+TR156)/(2.D0*A)
IF (GAMA2S.LE.O.DO) GO TO 800
       REGION
                                     2
                                                HYPERBOLIC CASE
                      V10=GAMA2*D(MN)
V11=DMEGA*BETA*EPS2/2.DO
V12=1.DO/(DTANH(V10))*GAMA2)
IF (V10.GE.170.DO) GO TO 14
V13=D(MN)/((DSINH(V10))*2)
                     V13=0(MN)/((DSINH(VIO)) ++2)

GO TO 15

V13=0.DO

V15=BETA/(2.DO*OMEGA*AMU2)

V14=ALFAN*6ETA/AKC2S

V16=(V14*522-EX2)**2+(-V14*521+EX1)**2

V17=(V14*6ZS-EZI*EXI-6Z2*EX2)

TR21=-V11*4LFAN**2*6ZS/(AKC2S**2)*(V12-V13)

TR22=-V15*ALFAN**2/GAMA2S*V16*(V12+V13)

TR23=-V15*V16*(V12-V13)

TR24=-V11*GAMA2S/(AKC2S**2)*(V12+V13)*EZS

TR256-ALFAN/(OMEGA*AMU2*AKC2S)*(BETA**2+AK2**2)*V17*V12

GO TU 801
       REGION 2 TRIGONOMETRIC
                                                                                          CASE
                     V25=1.DO/(AKC2S*DSIN(GAMA2*D(MN)))

V20=CMEGA*BETA*EPS2/2.DC

V21=0MEGA*BETA*AMU2/2.DO

DET1=V25*EZ2

DET5=-V25*EZ1

DETS=DET1**2+DET2**2

V26=ALFAN*BETA*V25/(DMEGA*GAMA2*AMU2)

V27=1.DO/(DMEGA*AMU2*GAMA2*DSIN(GAMA2*D(MN)))

CHT1=-V26*EZ2+V27*EX1

CHT2=-V26*EZ1-V27*EX1

CHT3=CV6*EZ1-V27*EX1

CHTS=CHT1**2+CHT2**2

V28=DSIN(2.DO*GAMA2*D(MN))/(2.DO*GAMA2)

TR21=-ALFAN*2*V20*DET5*(D(MN)-V28)

TR22=-ALFAN*2*V21*CHTS*(D(MN)-V28)

TR23=-(GAMA2**2)*V21*CHTS*(D(MN)-V28)

TR24=-(GAMA2**2)*V21*CHTS*(D(MN)-V28)

TR250=(BETA**2+AK2**2)*DET5*(D(MN)-V28)

TR250=(BETA**2+AK2**2)*DET5*(D(MN)-V28)

TR250=(BETA**2+AK2**2)*ALFAN/2.CO*(DET1*CHT1+DET2*CHT2)

PWR2=-(TR21+TR22+TR23+TR24+TR256)/(2.DO*A)
        300
                            POWER FLOW IN FREE SPACE REGION
        TCTAL
                       TTPWR1=TTPWR1+PWR1
        TOTAL POWER FLOW IN DIELECTRIC REGION
                       TTPWR 2=TTPWR 2+PWR 2
        TOTAL POWER FLOW
                       TOTPWR=TOTPWR+PWR1+PW82
C
                      GO TO 100
                   FZS=(R1**2-2.D0*R3+1.D0)/R2
GXS=((PI/(2.D0*W(M)))**2+4LF4N**2+ALF4N*PI/W(M)*DSIN
X(ALF4N*W(M)))/Q**2
                     (ALFAN# (M)))/Q**2
T1N=AM1 *GXS
T2N=AM4*FZS
B=-FZ1*GX2+FZ2*GX1
T3N=AM2*B
SUM1=SUM1+T1N
SUM2=SUM2+T2N
SUM3=T3N
CONTINUE
        100
C
                                  (S.EQ.1.DO) GO TO 19
(TOTPWR.NE.O.DO) GO
                                                                                                            TO
```

```
SUM3SQ=(SUM3) ** 2
TOT(K) = SUM1 * SUM2 + SUM3SQ
IF (DABS(TOT(1)) . LE.1.C+C1)
CONTINUE
                                                                                                                             GC TO 3000
   2000
                     DTOT=(TOT(2)-TOT(1))/DBETA

BETA1=DABS(BETA1-TOT(1)/DTOT)

IF (BETA1-LE-AK1) GO TC 50

GO TO 70

BETA1=BETA1+1.DO

GO TC 100

WVLNG=3.0D+8/FREQ(L)

RATIO=2.DO*PI/(BETA1*WVLNG)

WRITE (6,211) RATIG,D(MN),BETA

FORMAT (24X,F6.4,7X,E11.5,7X,E11.5)

GO TO 16

S=1.DO
           60
           50
           70
   3000
       SIGN=-1.DO , PROPAGATION IN BACKWARD DIRECTION (+Z)
                     SIGN=-1.DO
N1=1G1
I1=201
GC TO 9
S=0.DO
CONTINUE
CONTINUE
CONTINUE
    8000
   60 00
50 00
40 00
                      GO TO 8001
       STEP3- CALCULATIONS OF NORMALIZED PROPAGATION CONSTANTS AND ATTENUATIONS.
                     V14=BETA*ALFAN/AKC2S

V16=(V14*EZ2-EX2)**2+(-V14*EZ1+EX1)**2

V17=(V14*EZS-EZ1*EX1-EZ2*EX2)

V30=(BETA*ALFAN)**2+AKC2S**2

V30=(BETA*ALFAN)**2+AKC2S**2

V22=(OMEGA*EPS2*GAMA2)**2

V32=(OMEGA*EPS2*GAMA2)**2

V33=(SIGN)*2*O*V14*EPS2/AMU2*V17

V45=EPS2/AMU2*(EX1*5Z2-EX2*EZ1)

IF (GAMA2S*LE*O*D0) GC TG 22
           18
       HYPERBOLIC
                                              CASE
                     V10=GAMA2*D(MN)

V12=1.D07(DTANH(V10)*CAMA2)

IF (V10.GE.170.D0) GC 7C 24

V13=D(MN)/((DSINH(V10))**2)

GO TC 25

V13=0.D0

RE1=(V33+V34)*(V12+V13)/2.D0

ZM1=-QE1

ZM2-QE3

GO TC 23

GO TC 23
       TRIGONOMETRIC CASE
                     V40=D(MN)/(DSIN(GAMA2*D(MN))**2)

V41=1.DO/(DTAN(GAMA2*D(MN))*GAMA2)

RE1=(V32-V34)*(V4C+V41)/2.DO

ZM1=-RE1-V45*(V40+V41)

ZM2=-RE3

ZE11=RE11+9E1

RE22=RE22+RE3

ZM11=ZM11+ZM1

ZM21=ZW21+ZM2

GO TC 100
           22
0
```

```
G1=2.8D6*PI*G

CMGAM=G1*AMAGS

GMGAO=G1*HO

CMGAR=CMGAO-CMGAM

DAMP=G1*DELTH/(2.DO*CMEGA)

DELT=(CMGAR**2-CMEGA**2*(1.DO+CAMF**2))**2+

X4.DO*(CMGAR**CMEGA**CAMP)**2
      CALCULATION OF SUSCEPTIBILITY TENSOR'S COMPONENTS
                    XXX1=0MGAM*0MGAR*((3MGAR**2-0MEGA**2)+(2MEGA*DAMP)**2)

XXX2=0MGAM*0MEGA*DAMP*(CMGAR**2+0MEGA**2*(1.0C+CAMP**2))

XXX1=0MEGA*3MGAM*((3MGAR**2-0MEGA**2*(1.0C+DAMP**2))

XXZ1=0.00*0MEGA**2*0MGAM*(2MGAR**2-0MEGA**2*(1.0C+DAMP**2))

XXZ2=2.00*0MEGA**2*0MGAMP*CMGAR

XZ2=2.00*0MEGA**2*XXI

XZ2=2.00*0MEGA**2*XXI

XZ2=2*XX1*RE11+RE22*XXXI

ZM=XXX2*ZM11+ZM21*XXZ2

EORMAT (///)

WRITE (6,904)
       904
C
      V50=0MEGA*AMU1/(4.CO*TOTPWR*DELT*A)
ATTEN=-ZM*V50
D5=8.68589638D-02*ATTEN
BETAP=BETA+RE*V50
RAT=BETAP/BETA
IF (SIGN.EQ.1.D0) GO TC 81
WRITE (6,898) DB
WRITE (6,898) DB
GS8 FORMAT (10X.21HBACKWARC ATTENUATION=,E11.5,6H CB/CM//)
MRITE (6,897) RAT
S57 FORMAT (10X,21HBETAF/BETA BACKWARC =,E10.4//)
       SIGN=+1.DO .PROPAGATION IN FORWARD DIRECTION
                    SIGN=+1.DO
GD TO 8000
WRITE (6,900) DB
WRITE (6,990) DB
FORMAT (10x,20HFDRWARD ATTENUATION=,511.5,6H DB/CM//)
WRITE (6,399) RAT
FORMAT (10x,20HBETAF/BETA FORWARD =,510.4//)
       900
       899
    8001
                     STOP
```

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